



# **Jason 3 GPS orbits with ambiguity fixing**

**Flavien Mercier (CNES), Hanane Ait Lakbir (CS-SI), Alexandre Couhert (CNES)**

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# Summary

## Introduction

### Some Jason 3 receiver characteristics

- pseudo-range biases
- widelane properties

### Zero difference ambiguity fixing

- method
- global statistics

### Orbit performance

- GRD-E orbit comparisons
- normal bias
- SLR residuals

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## Context

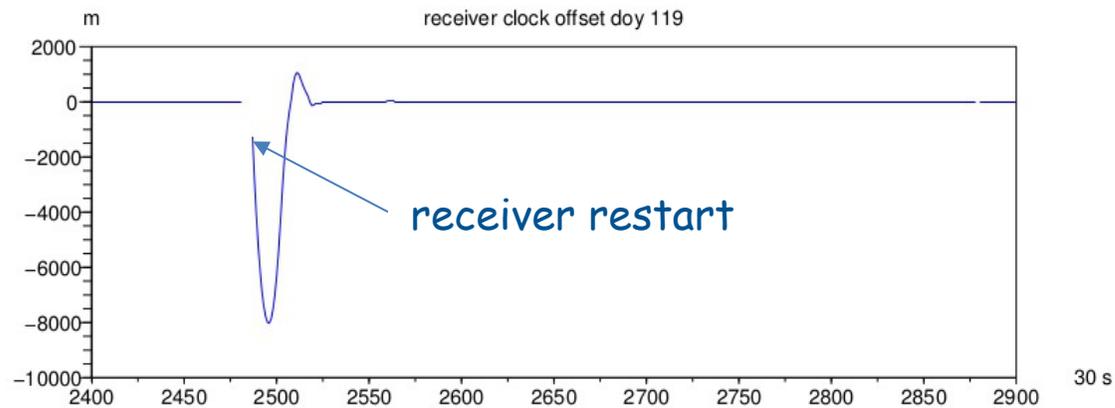
GPS receivers on altimetry satellites

- **Jason 1** : the possibility of ambiguity fixing has been demonstrated (2004, double differences (JPL), 2009, zero differences (CNES))
- **Jason 2** : half cycles ambiguities, half cycle slips (SNR issues), reliable ambiguity fixing not possible
- **HY2A** : correct ambiguity fixing (2012, not operationally implemented)
- **Sentinel 3A** : half cycle ambiguities observed in the CPOD rinex files, reliable ambiguity fixing not possible

For **Jason 3** : very good quality of the measurements, no more SNR problems  
zero difference ambiguity fixing operational orbits are possible (2017)

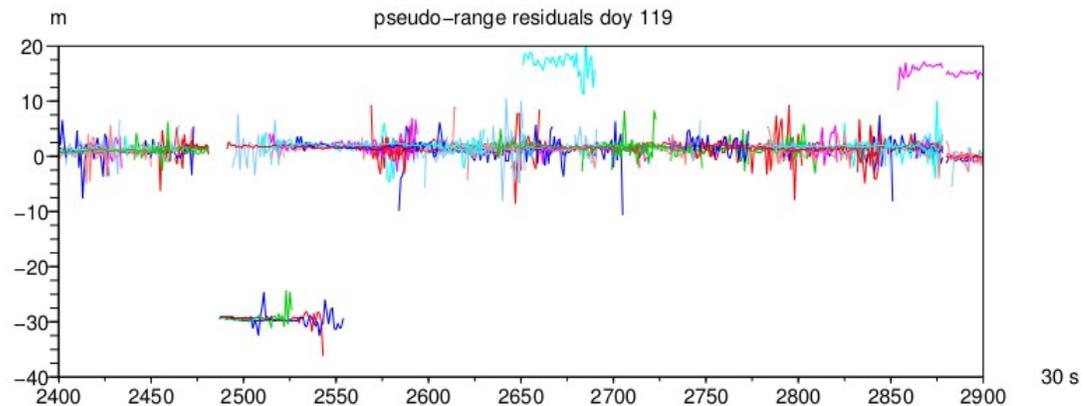
# Jason receiver measurements characteristics

Receiver clock



Pseudo-range residuals

(solution with downweighted pseudo-range)

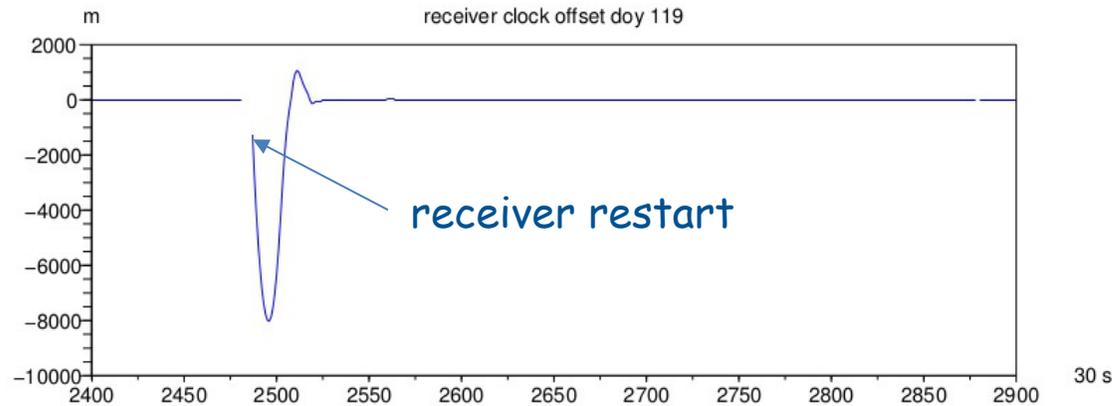


# Jason receiver measurements characteristics

Pseudo-range biases :

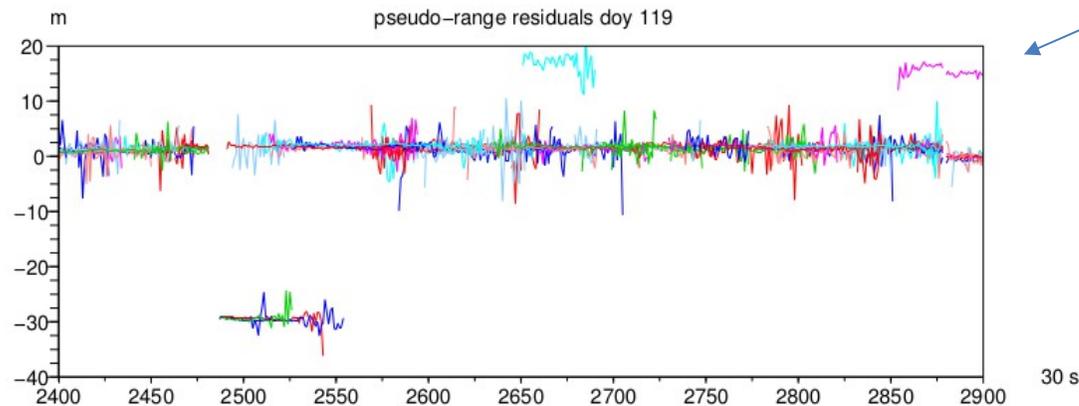
- some isolated passes biased (15 meters), on C1,P1,P2

Receiver clock



Pseudo-range residuals

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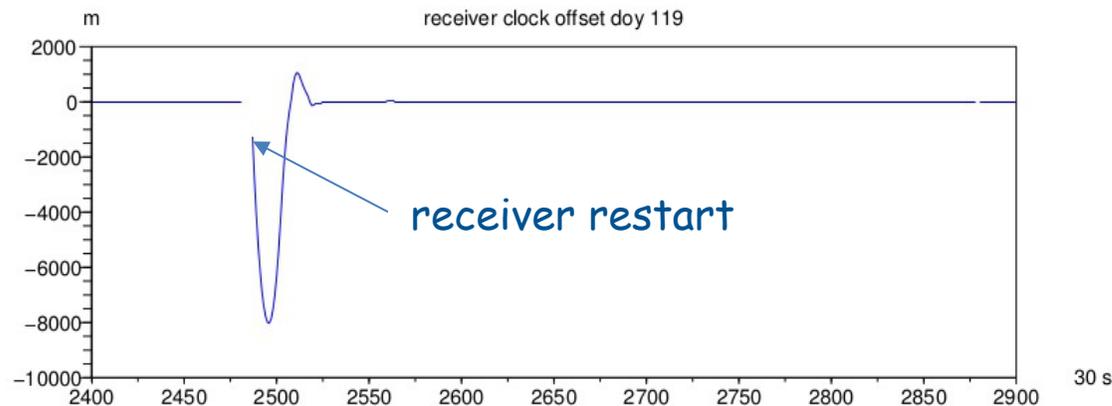


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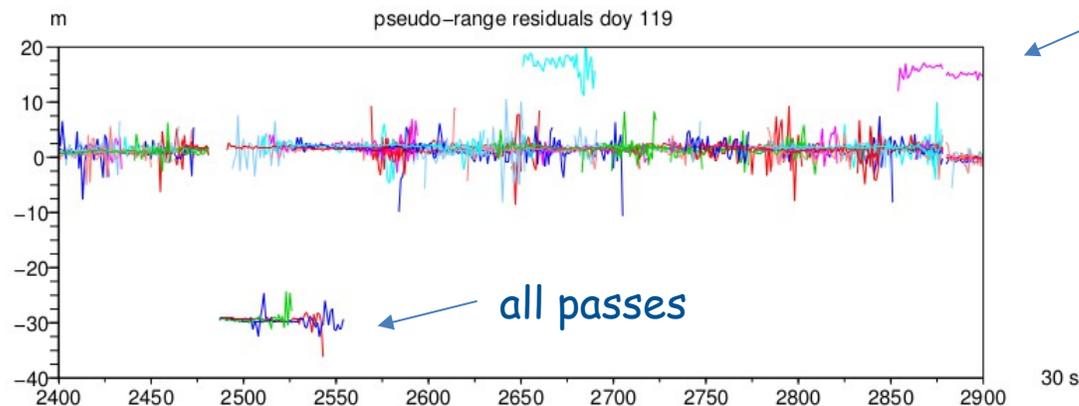
- some isolated passes biased (15 meters), on C1,P1,P2
- systematic simultaneous biases observed during receiver restarts, on C1,P1,P2

Receiver clock



Pseudo-range residuals

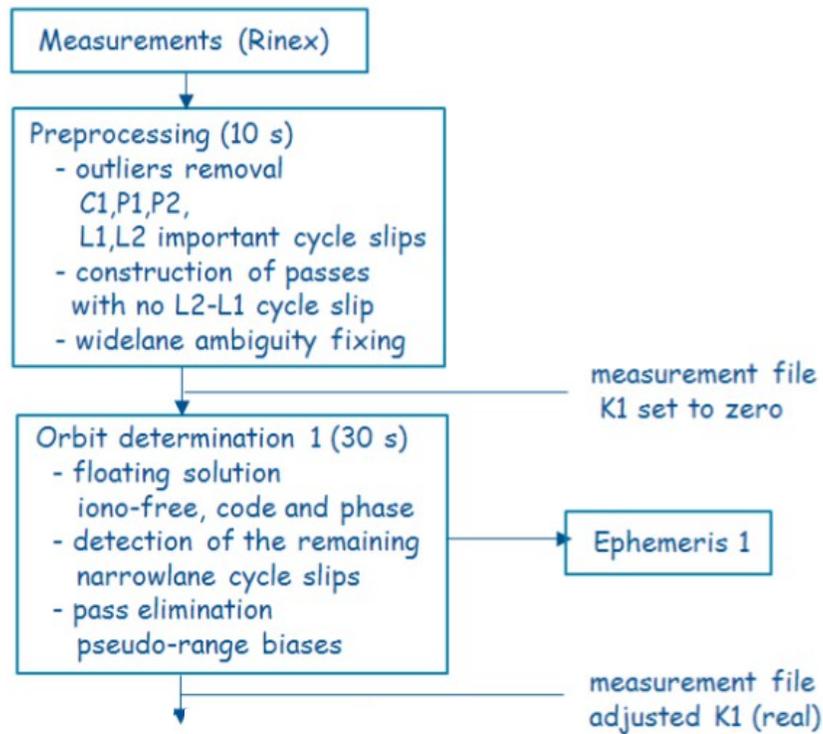
(solution with downweighted pseudo-range)



one pass

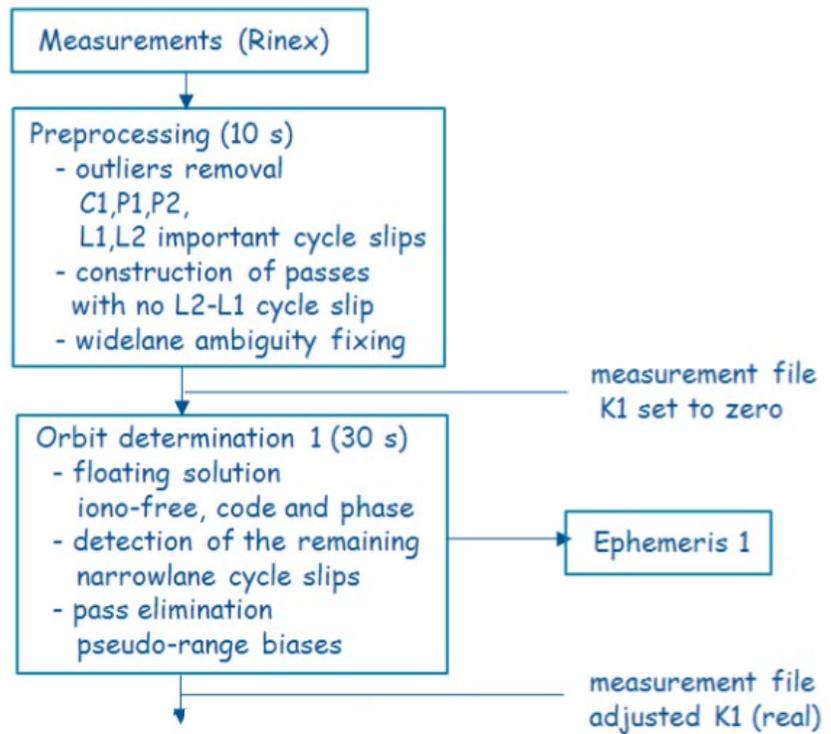
# Complete process

## Initial solution (floating K1 ambiguities)

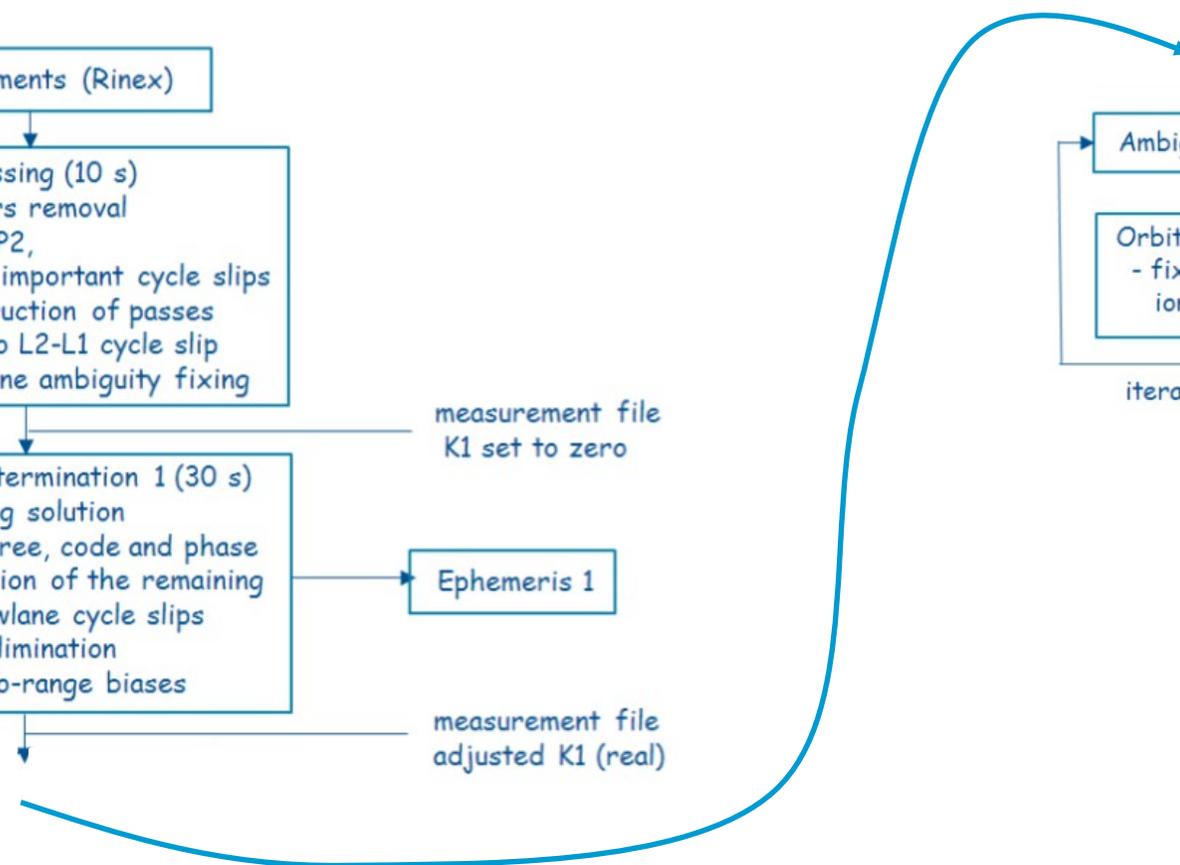
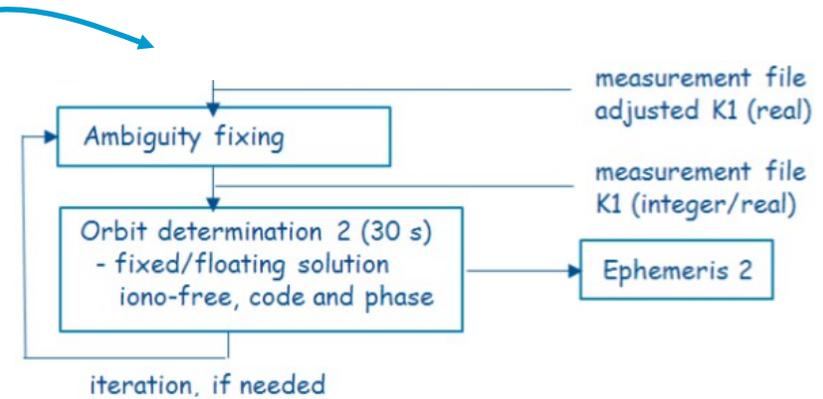


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## Initial solution (floating K1 ambiguities)

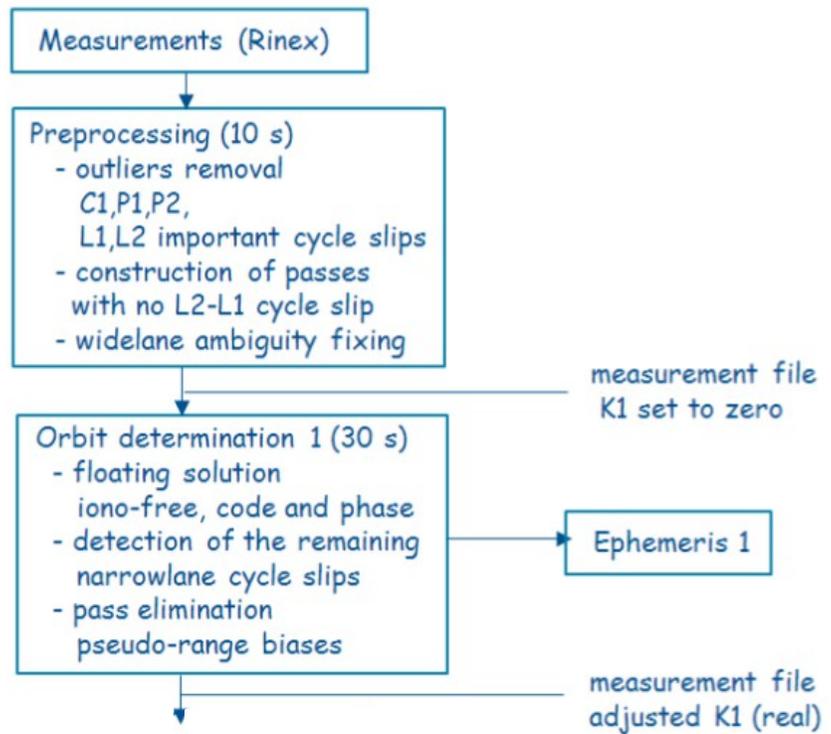


## K1 fixing ('Narrowlane')

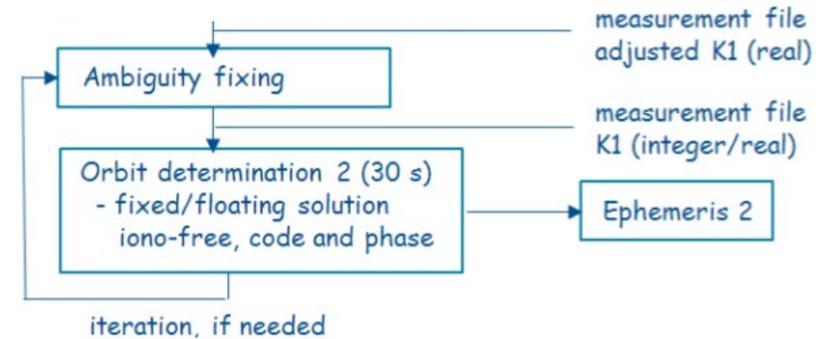


# Complete process

## Initial solution (floating K1 ambiguities)



## K1 fixing ('Narrowlane')



The final measurement file can be used in other configurations

Rapid solutions :  
equivalent to code only solution

Longer arcs : other dynamical models ...

# Orbit parameterization for fixing (floating ambiguities)

Parameterization :

Direction	type	number of segments	duration
Tangential	1/rev	2	14 hours
	constant	13	2 hours, 3 hours at the ends of the arc
Normal	1/rev	2	14 hours
	constant	2	14 hours

Phase : 2 cm

Pseudo-range : 2 m

Phase map : JPL pre-launch phase map

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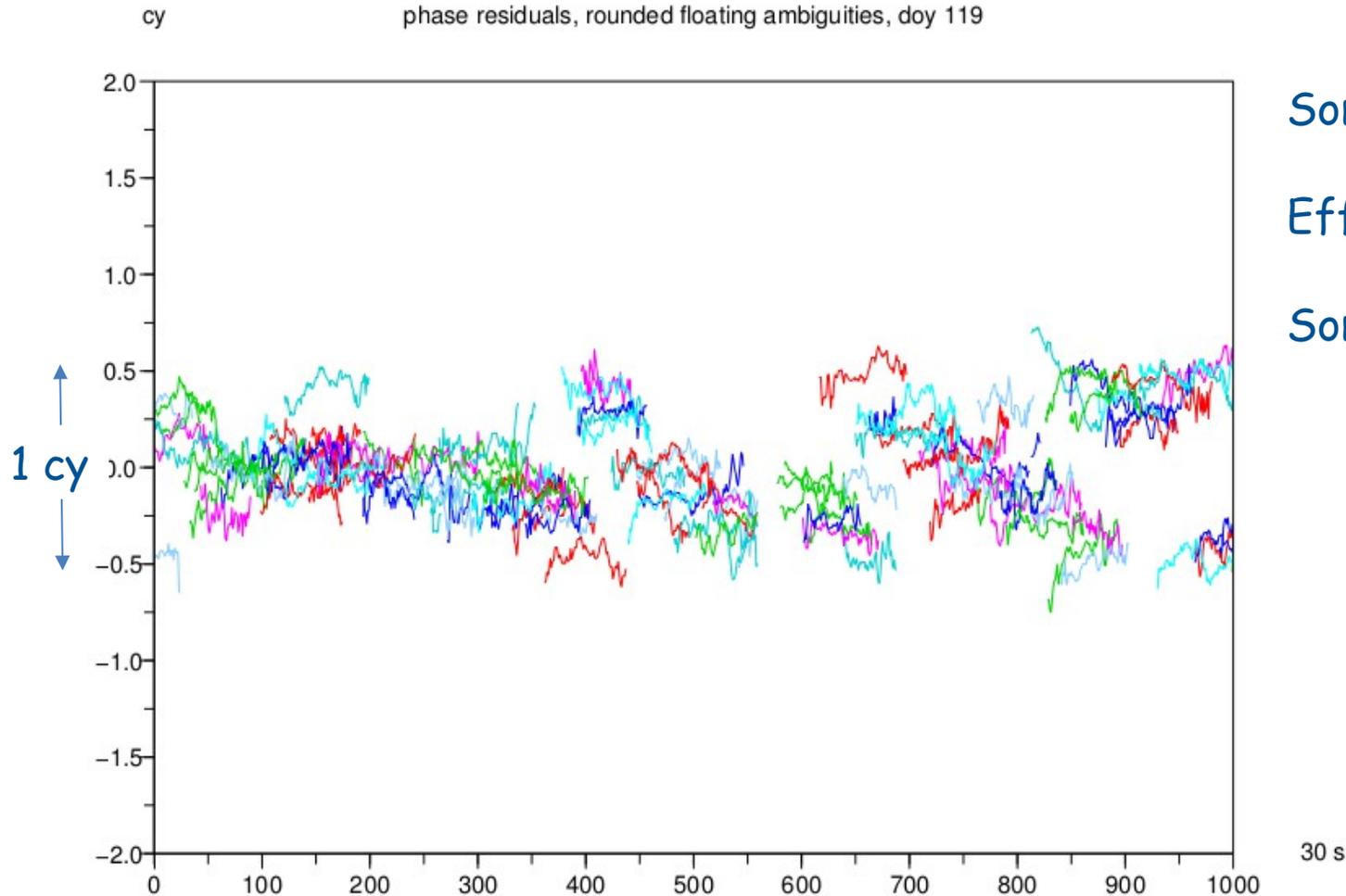
Phase : 2 cm

Pseudo-range : 2 m

Phase map : JPL pre-launch phase map

A normal constant empirical acceleration was needed for good ambiguity fixing rates

# Phase residuals, rounded floating ambiguity

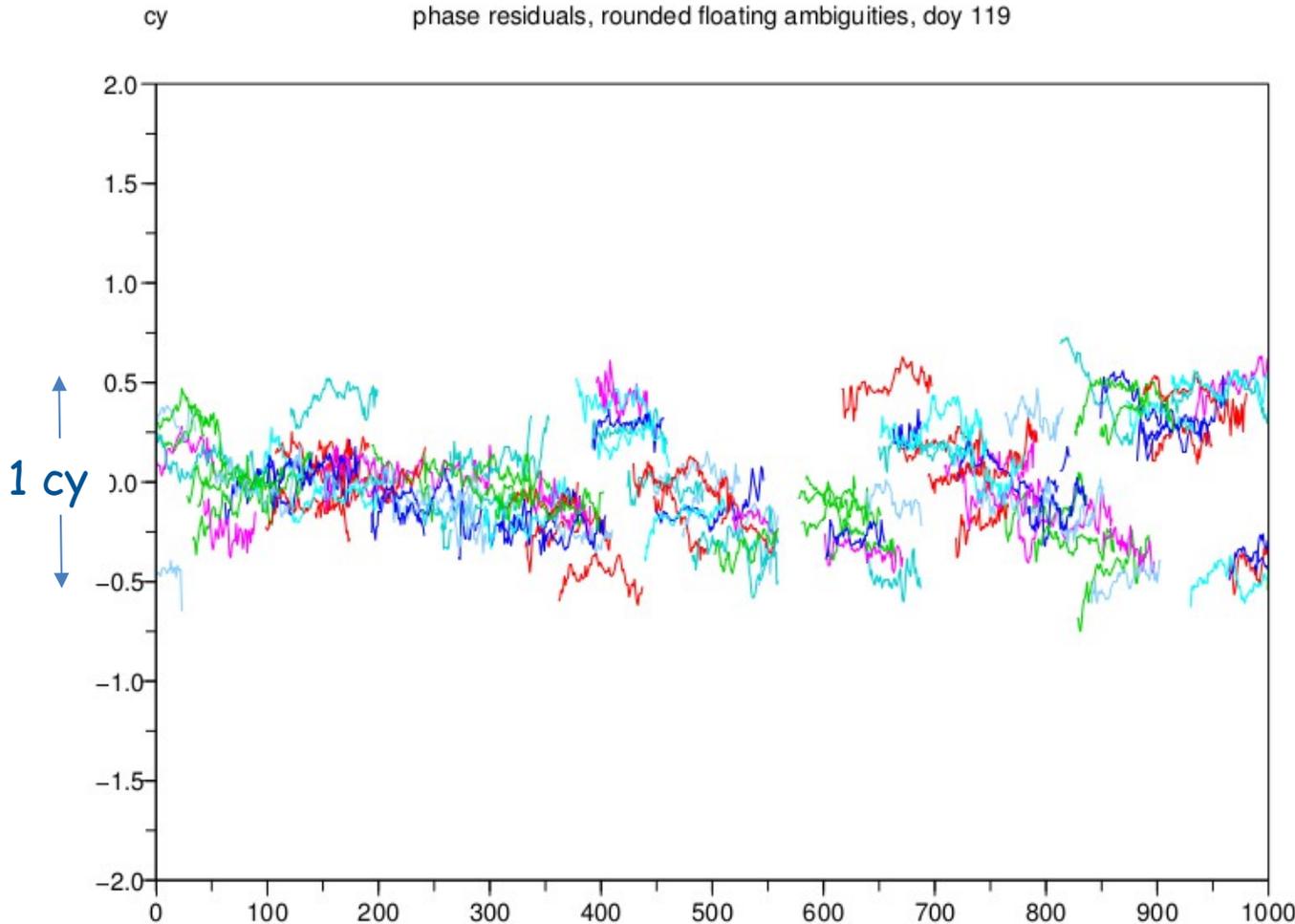


Some passes can be fixed

Effect of the coupling with the clock

Some passes have non integer ambiguities

# Phase residuals, rounded floating ambiguity



Some passes can be fixed

Effect of the coupling with the clock

Some passes have non integer ambiguities

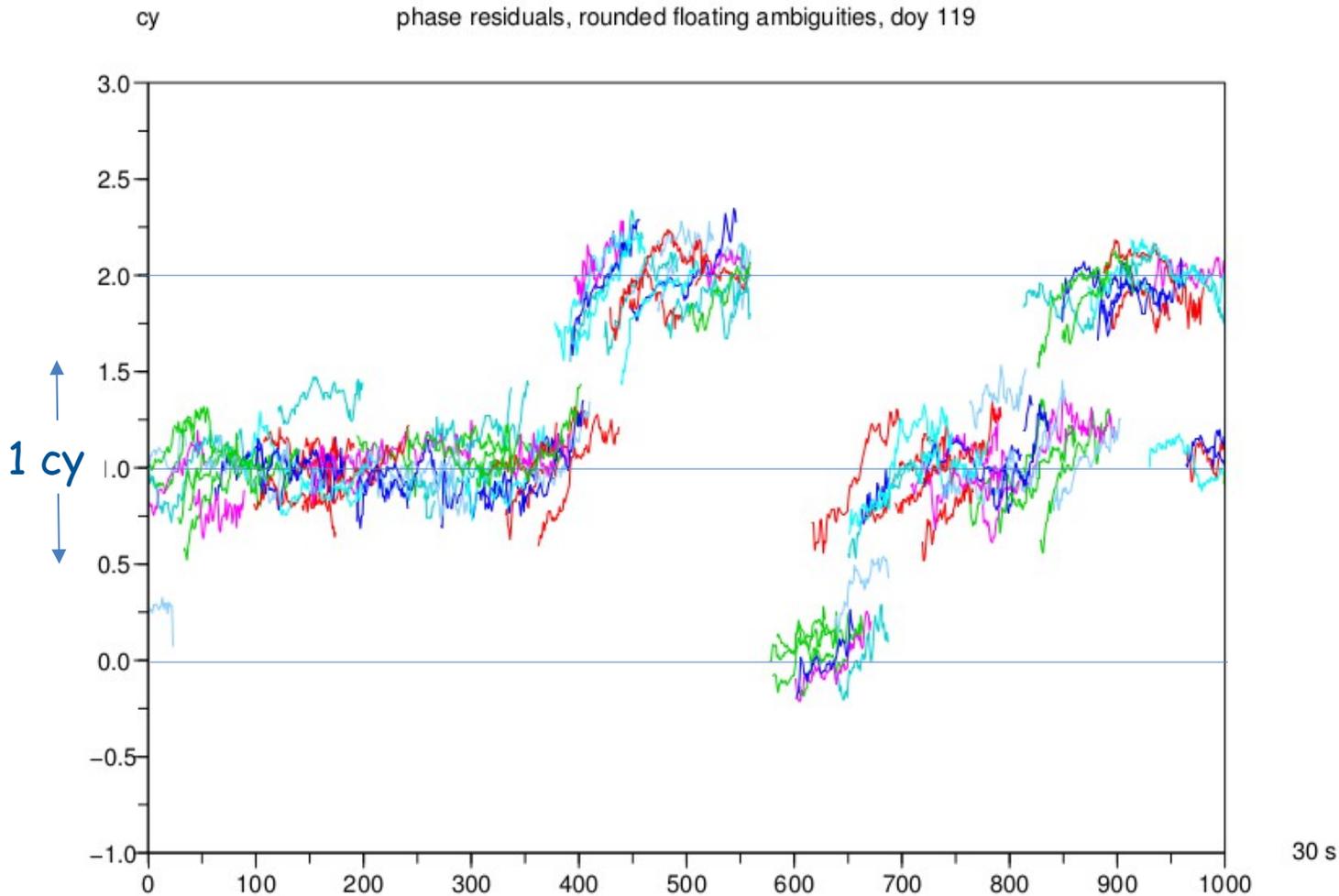


Simultaneous solution

- clock offset
- integer ambiguities

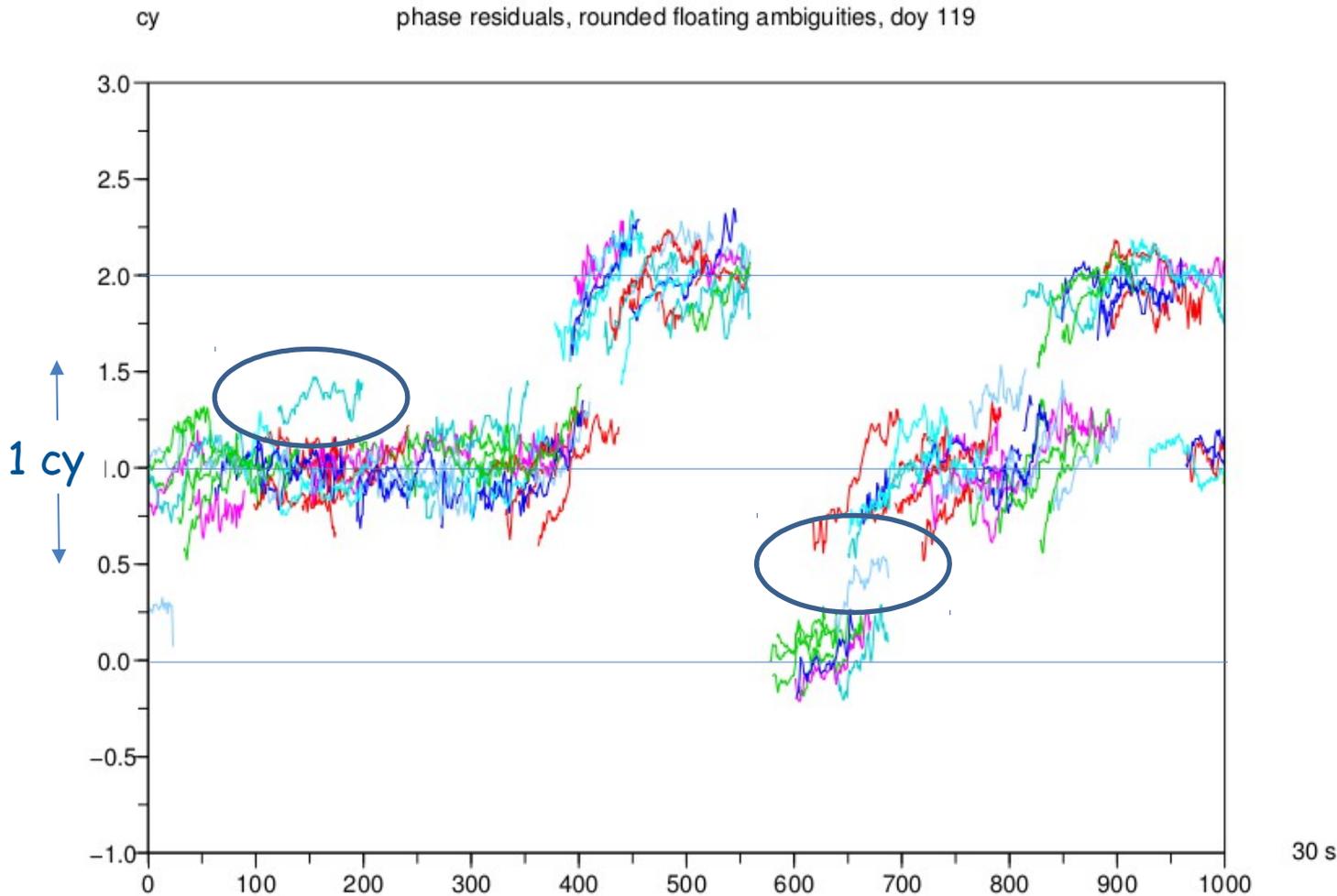
All passes

# Phase residuals, integer ambiguities and clock solution



The ambiguities are fixed

# Phase residuals, integer ambiguities and clock solution



The ambiguities are fixed

Some passes have important residuals

- receiver anomaly ?
- wrong widelane fixing
- GRG clocks anomaly

# Statistics (cycles 8-52)

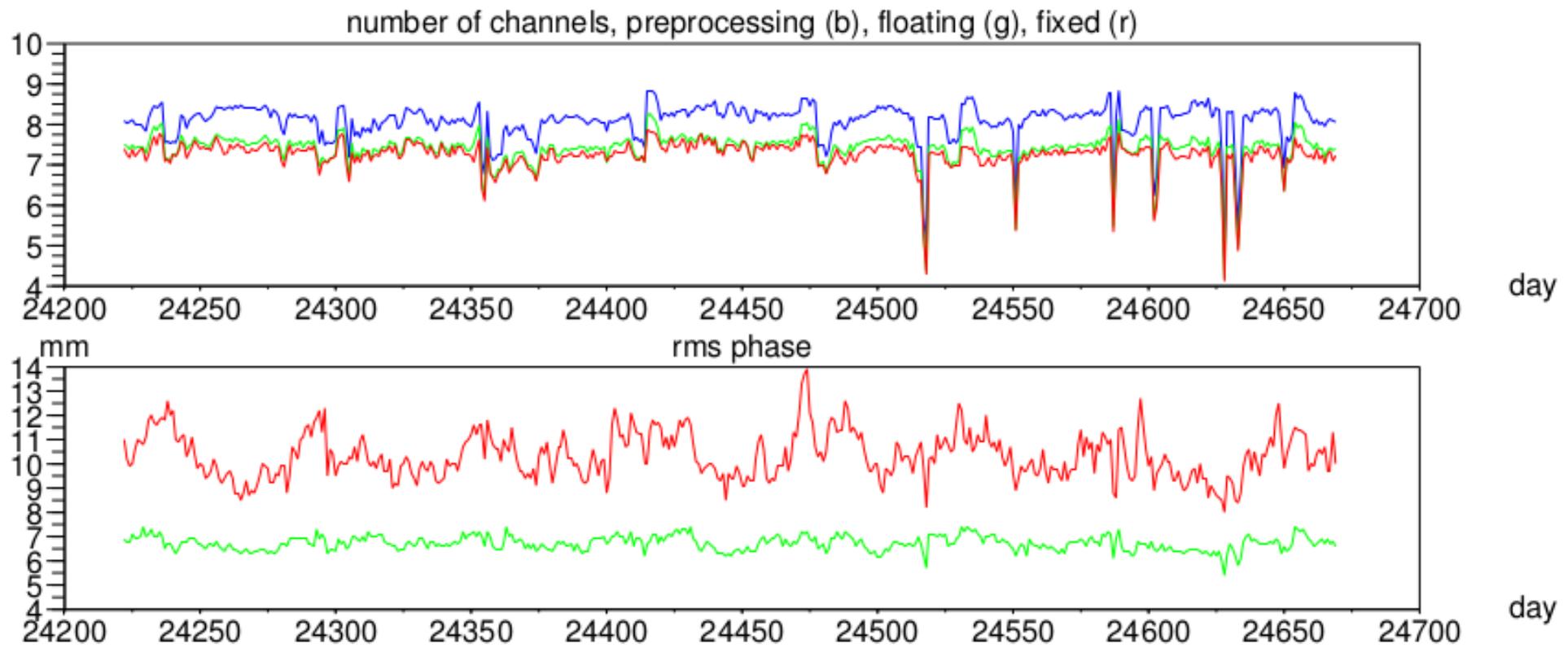
initial data

floating solution

(some eliminations, pseudo-range biases...)

fixed solution

(fixed amb. only)



# Attitude effects (cycles 8-52)

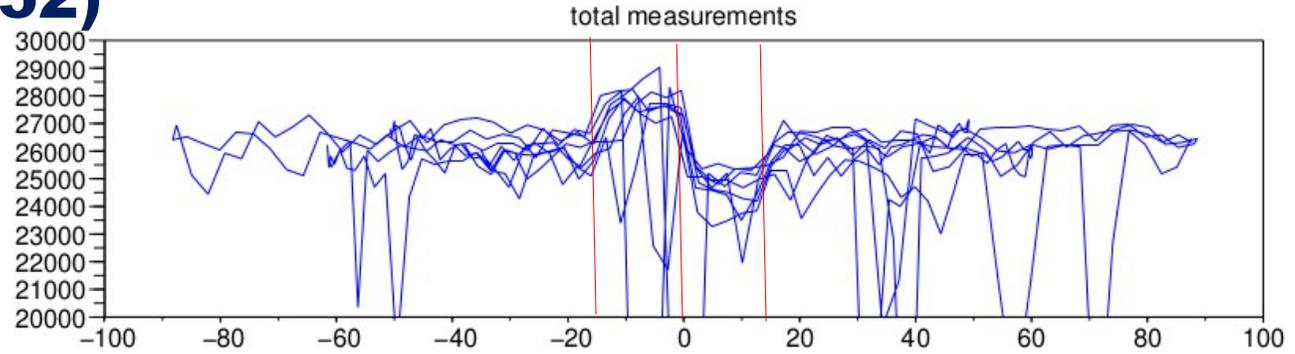
measurements

-15-0 degrees : backward  
more measurements  
fixing ratio ~97 %

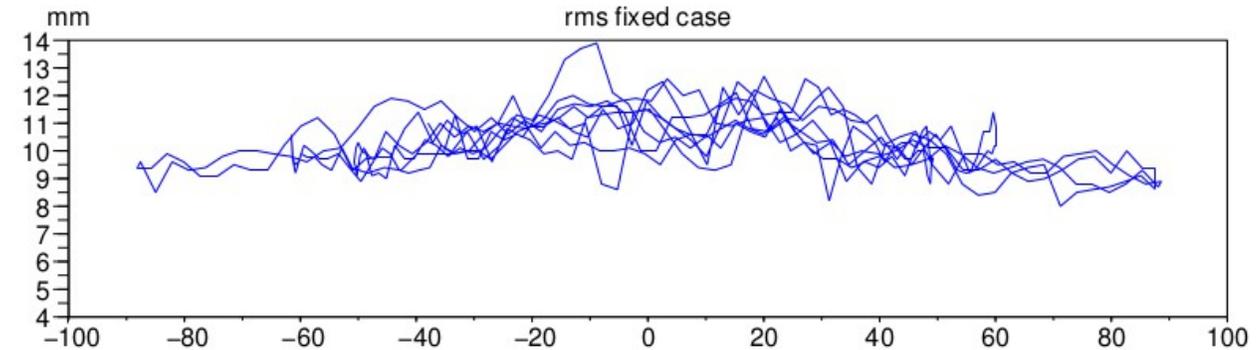
0-15 degrees : forward  
less measurements  
fixing ratio ~99 %

Fixing ratio not symmetric  
better for beta < -15

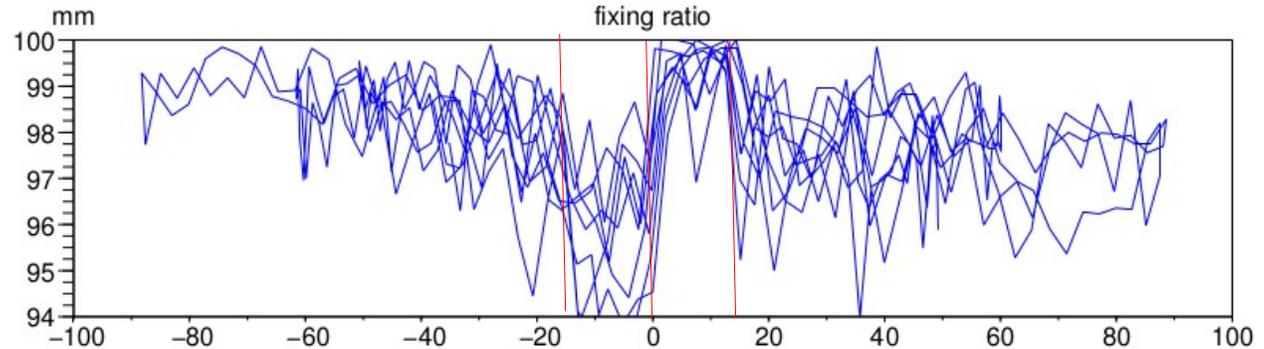
fixing ratio



$\beta$



$\beta$

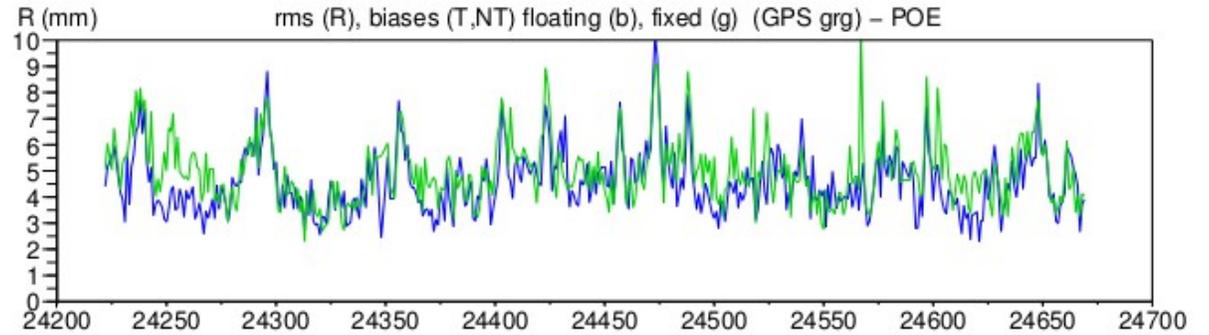


$\beta$

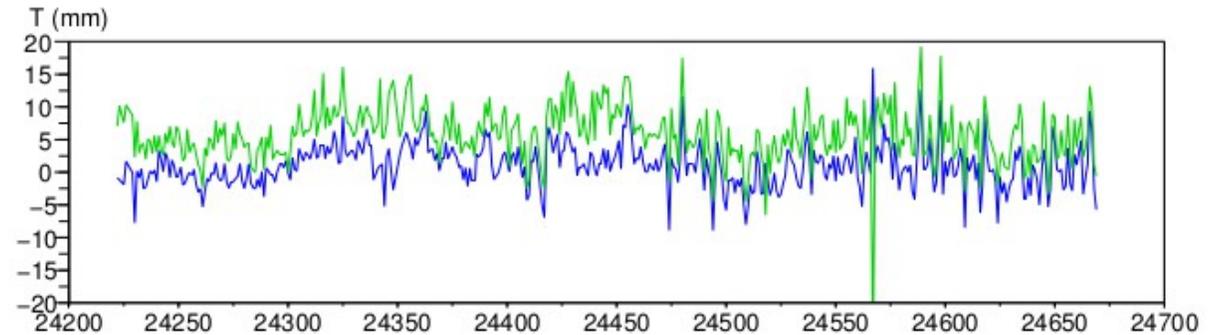
# Comparison with GDR-E

Radial rms  
floating, fixed 10 mm

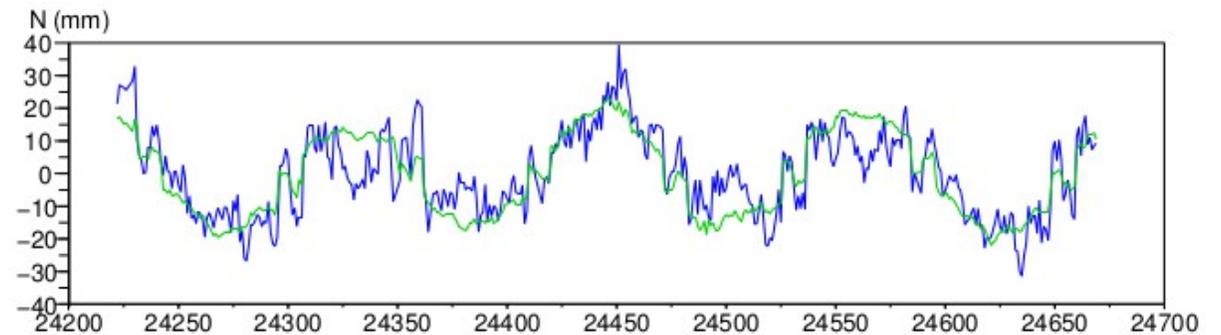
Equivalent radial rms



jj



jj



jj

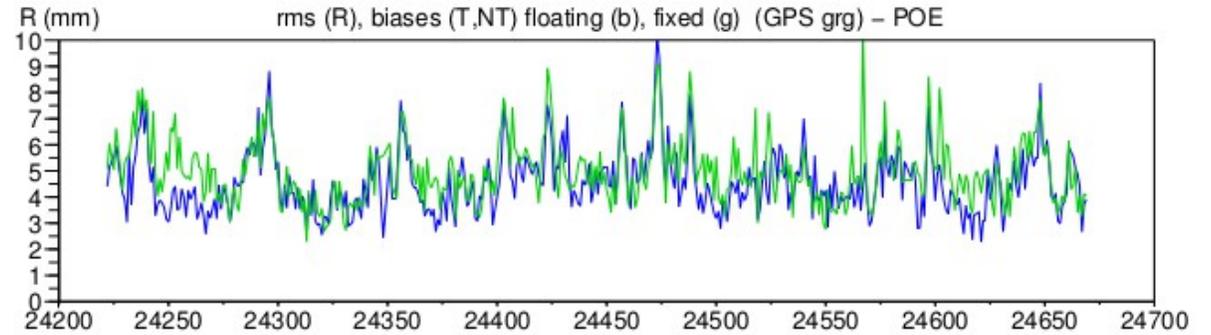
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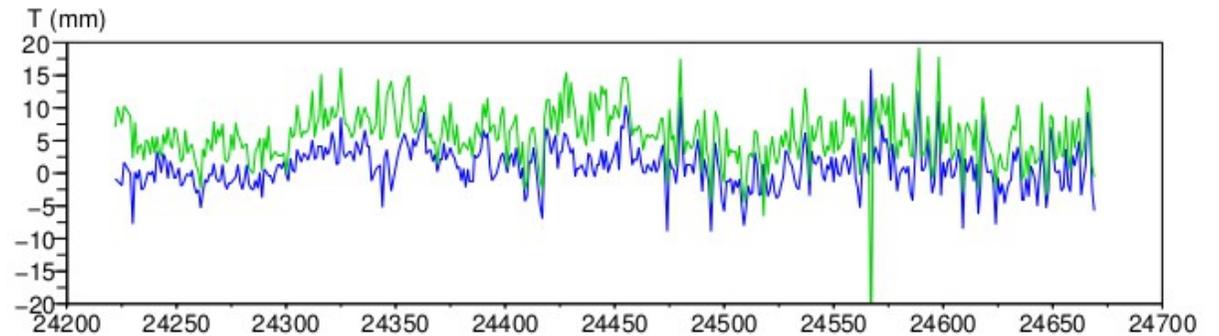
Equivalent radial rms

Tangential  
(bias ~5 mm) 20 mm

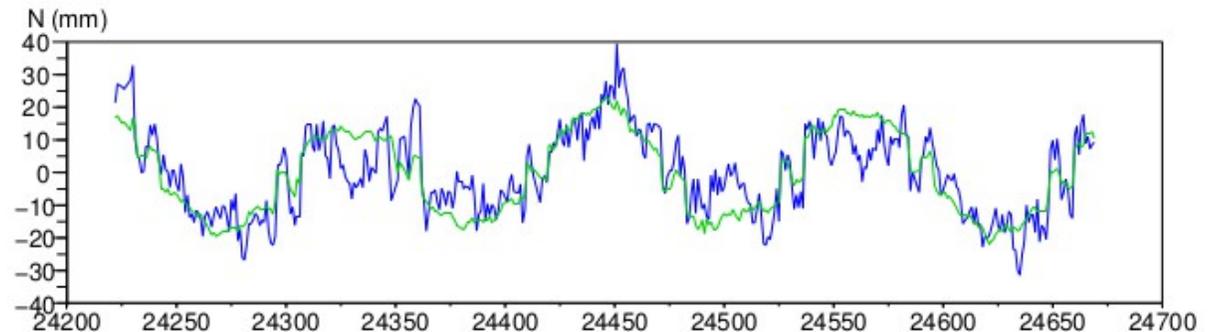
Bias due to underweighting  
of the pseudo-range in floating solutions



jj



jj



jj

# Comparison with GDR-E

Radial rms  
floating, fixed 10 mm

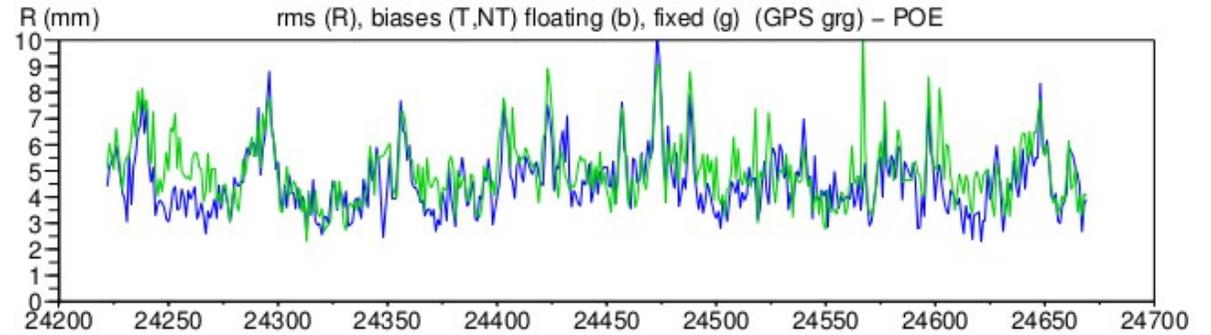
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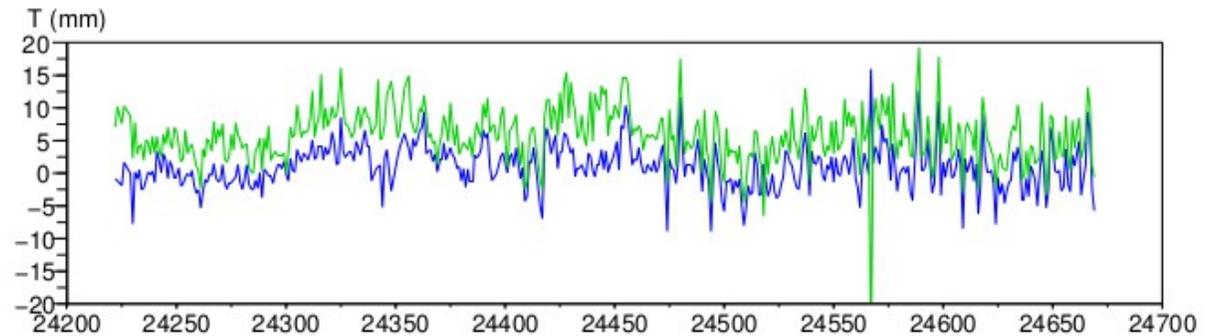
Bias due to underweighting  
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Normal  
40 mm

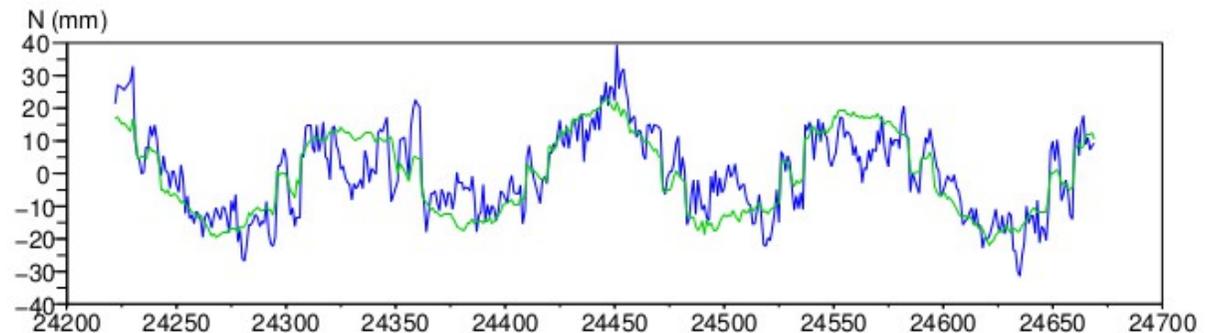
Important errors in the normal  
direction, beta angle dependency



jj



jj

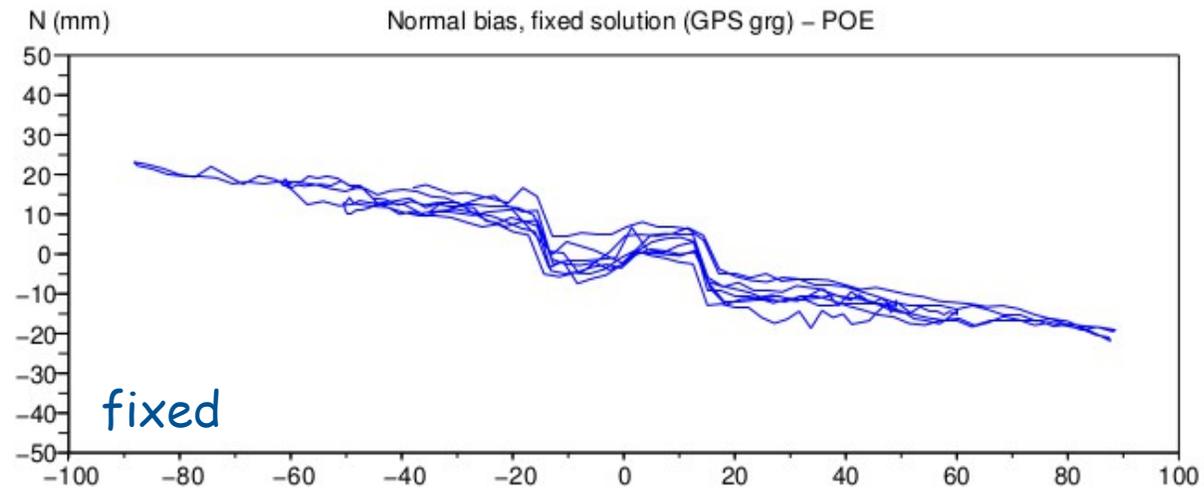
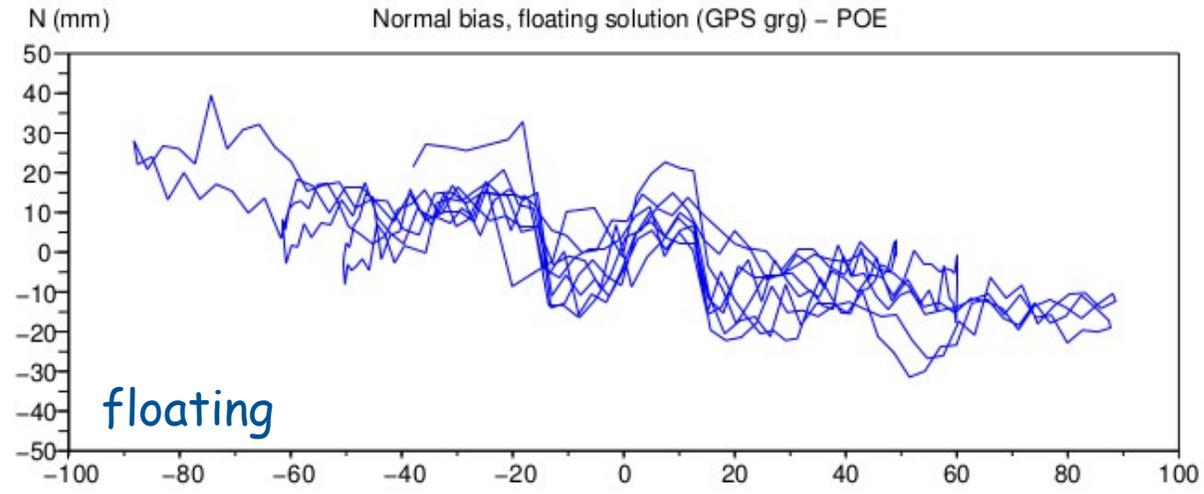


jj

# Normal bias function of beta

Possible error in the geometry  
or in the SRP model ?

40 mm



# Normal bias function of beta

40 mm



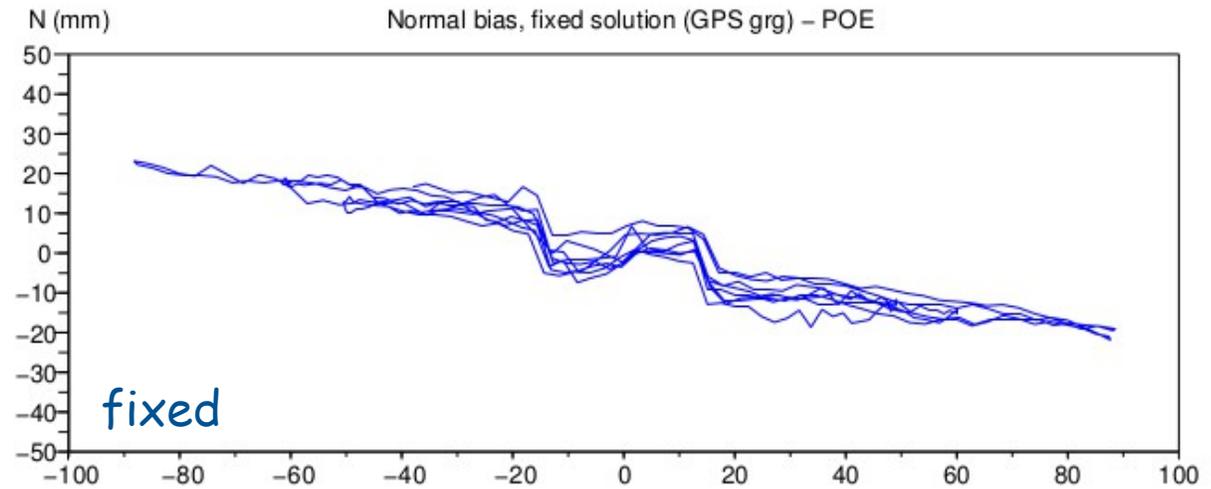
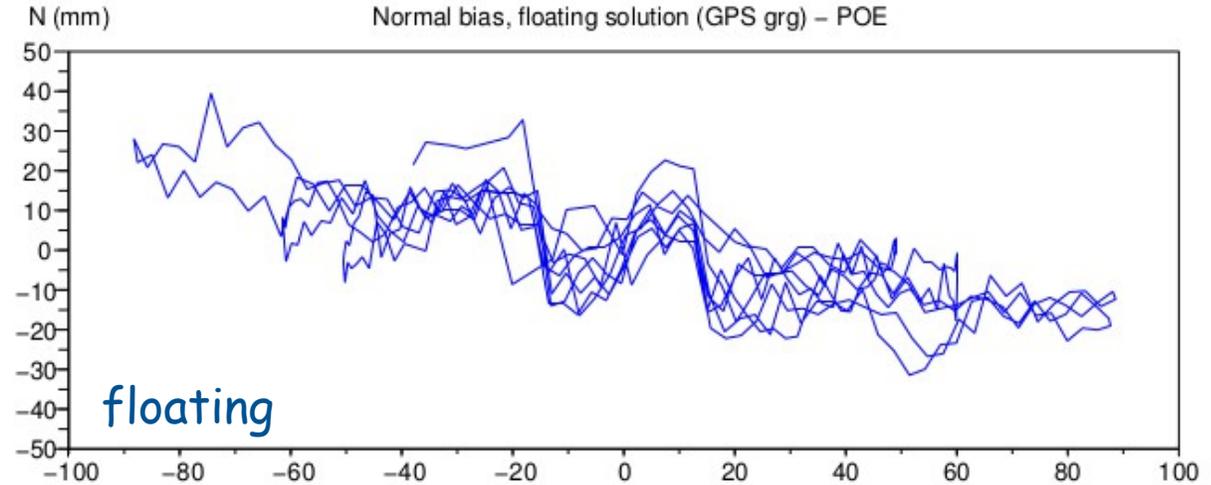
Possible error in the geometry  
or in the SRP model

The current SRP model is correct for  
the in-plane behaviour

error in the x-antenna location ?  
(high beta values, 2 cm bias)

Fixed yaw cases

5 mm, radiation pressure, y-antenna ?



jj

jj

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## SLR residuals analysis

Different solutions :

- current solutions, using JPL orbits/clocks (GDR-E standards)

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## SLR residuals analysis

Different solutions :

- current solutions, using JPL orbits/clocks (GDR-E standards)
- new solution, floating, (JPL orbits/clocks)
- new solution, floating, (JPL orbits/clocks), normal bias adjusted

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## SLR residuals analysis

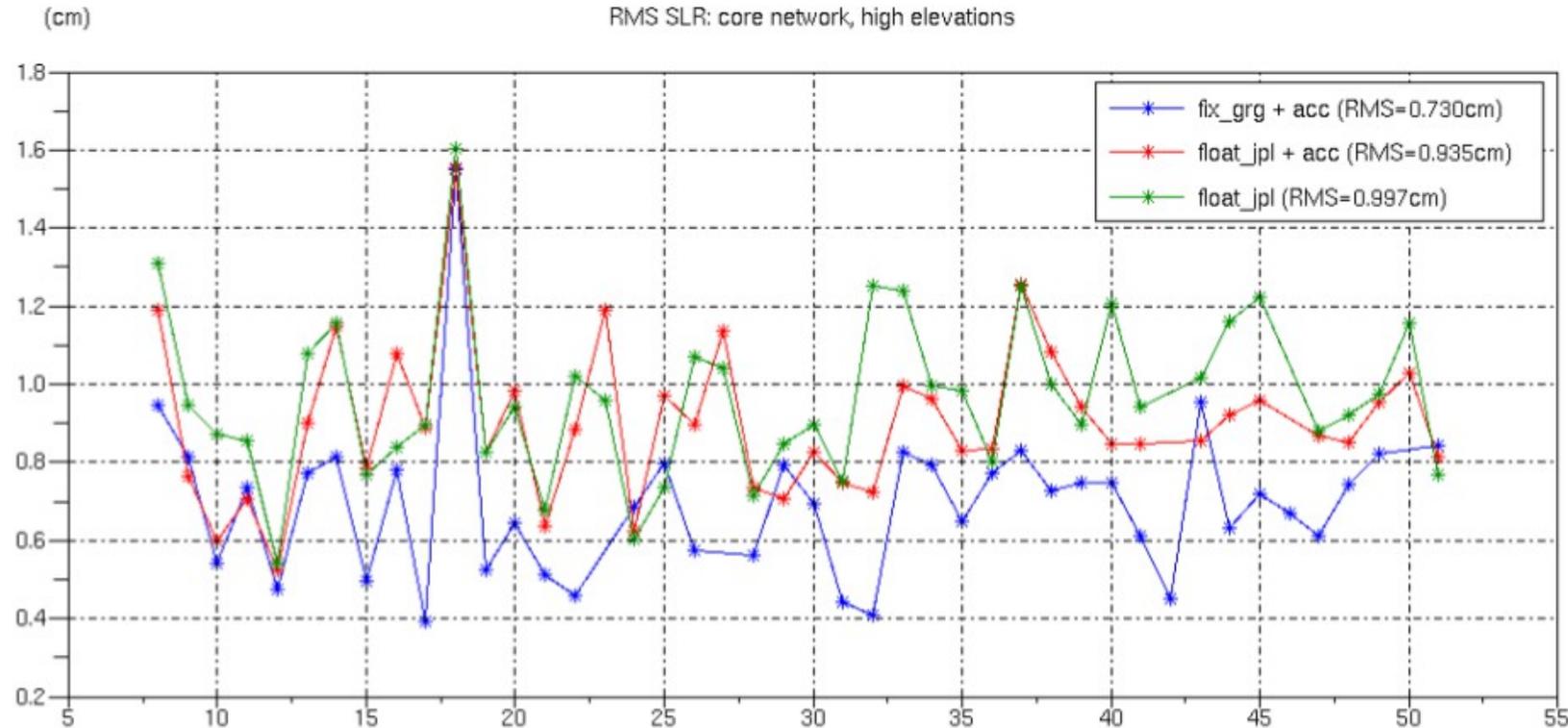
Different solutions :

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- new solution, floating, (JPL orbits/clocks), normal bias adjusted
- new solution, fixed, (GRG orbits/clocks), normal bias adjusted

Analysis of SLR high elevation residuals, core network

# SLR residuals, high elevations, core network, new solutions

Floating, no normal bias 10.0 mm  
 Floating, normal bias 9.4 mm  
 Fixed, normal bias 7.3 mm



Significant improvement for the high elevation SLR residuals due to :

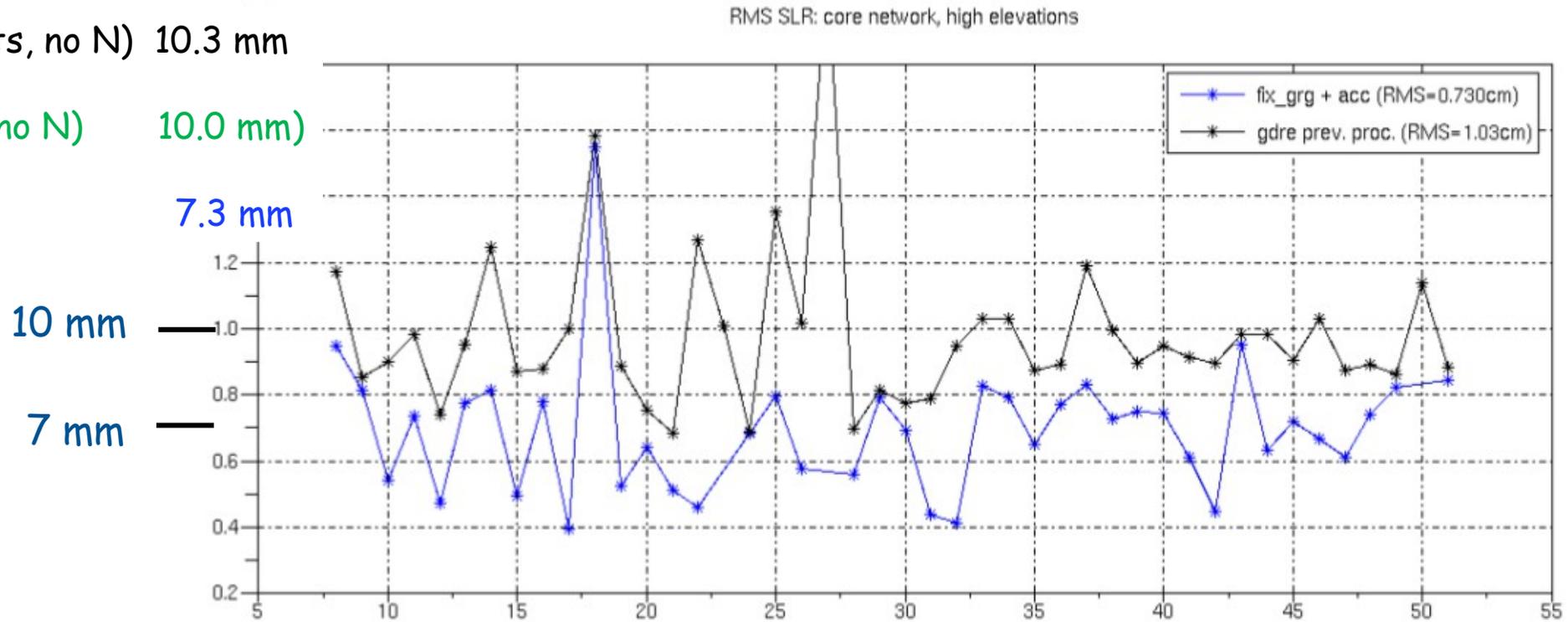
- normal bias
- fixed ambiguities

# SLR residuals, core network, high elevations, new/old orbits

Floating (current orbits, no N) 10.3 mm

(Floating (new orbits, no N) 10.0 mm)

Fixed, normal bias 7.3 mm



Small improvement for same kind of parametrization (float, no normal bias)

Significant improvement with fixed and normal bias : 3 mm better

Almost all cycles are now below 8 mm rms

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## Conclusion

Jason 3 orbits with zero difference ambiguity fixing

- use IGS grg solution (CNES/CLS analysis center) for GPS orbits and clocks
- high fixing ratios (> 95 %), but dependencies with the attitude law
- the process can work operationally

New orbits (GDR-F preliminary), with fixed ambiguities

- are close to the GDR-E orbits (5 mm rms radial)
- correct the observed along track bias, consistent with Doris now.
- normal direction accelerations (radiation pressure, or antenna location ?)
- better SLR residuals rms (all elevations and high elevations)

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Significative improvements of the SLR high elevation residuals (cycles 8-51)

Current orbits : 10.3 mm

New orbits : 7.3 mm 30% improvement

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## Further work

Normal bias :

investigations for the origin of this bias

- SRP ?
- GPS centre of phase ?
- ...

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Normal bias :

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Measurement processing

passes with erroneous K1 (widelane, pseudo-range biases, ...)

high rms flying backward, small rms flying forward

higher fixing ratio flying forward, but less passes

investigations :

- widelane anomalies ?
- measurement weighting, elimination of low horizontal elevation measurements ?
- phase map improvement (phase map estimation with fixed ambiguities) ?
- consequences for yaw steering phases

**Thank you**



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- HY2A : correct ambiguity fixing (2012, not operationally implemented)
- Sentinel 3A : half cycle ambiguities observed in the CPOD rinex files, reliable ambiguity fixing not possible

For Jason 3 : very good quality of the measurements, no more SNR problems  
zero difference ambiguity fixing operational orbits are possible (2017)

# Jason receiver measurements characteristics

Average number of channels (28 h)

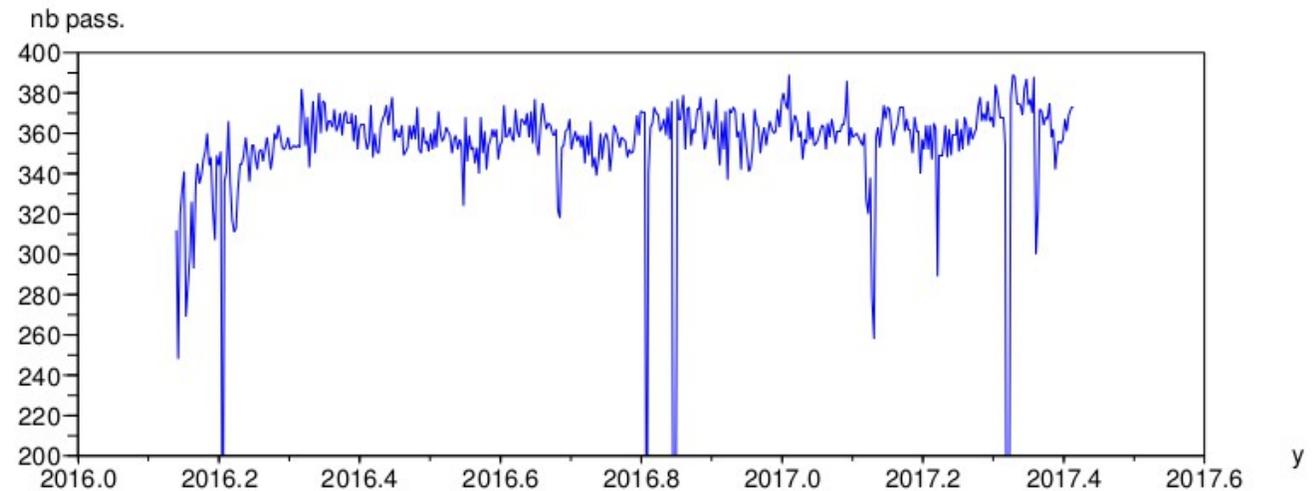
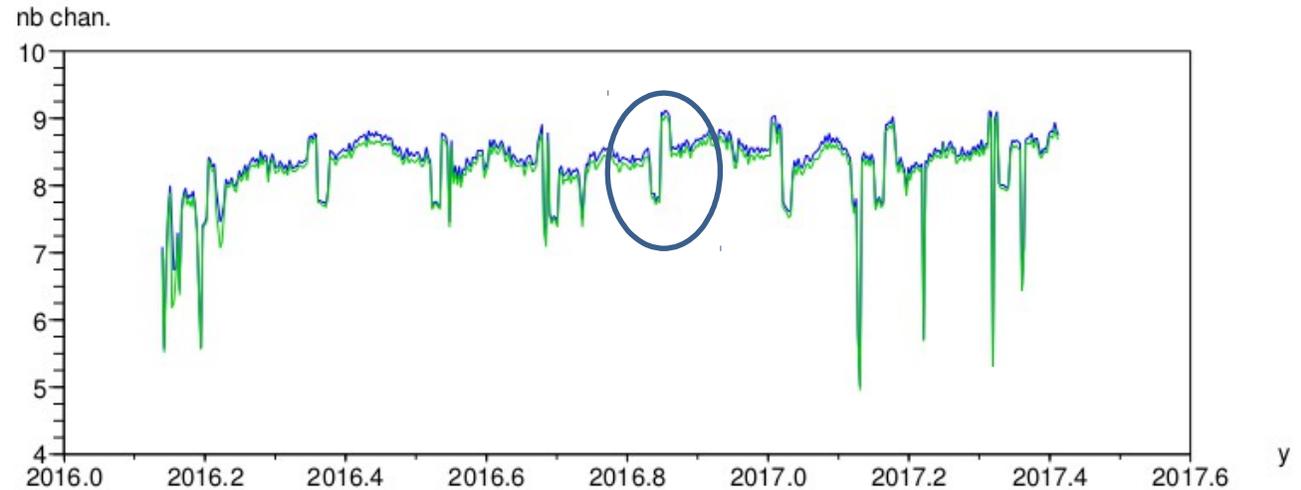
- initial
- used

Attitude law effects

- fixed, backwards ~8.5 chan.
- fixed, forward ~7.5 chan.
- yaw-steering ~8 chan.

Limitation : 10 deg elevation  
relative to antenna axis

number of passes (28 h)



## widelane (Melbourne – Wubbena) ambiguity fixing

Iono-free and geometry-free combination,  
Used for L2-L1 ambiguity determination, integer value  $K_w$  for each pass

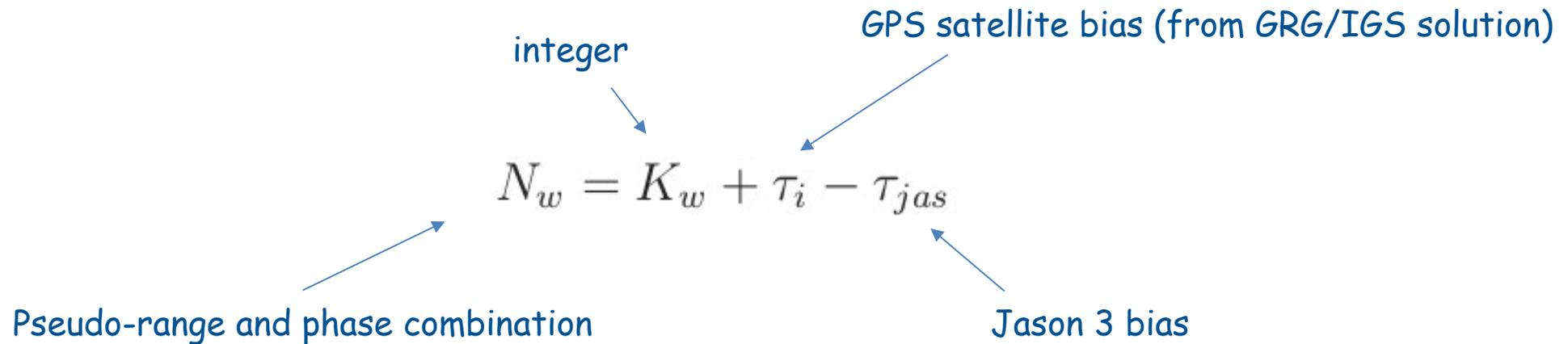
$$N_w = K_w + \tau_i - \tau_{jas}$$

integer

GPS satellite bias (from GRG/IGS solution)

Pseudo-range and phase combination

Jason 3 bias



# widelane ambiguity fixing results

Good stability of  $\tau_{jas}$

(constant value ?)

1 cy

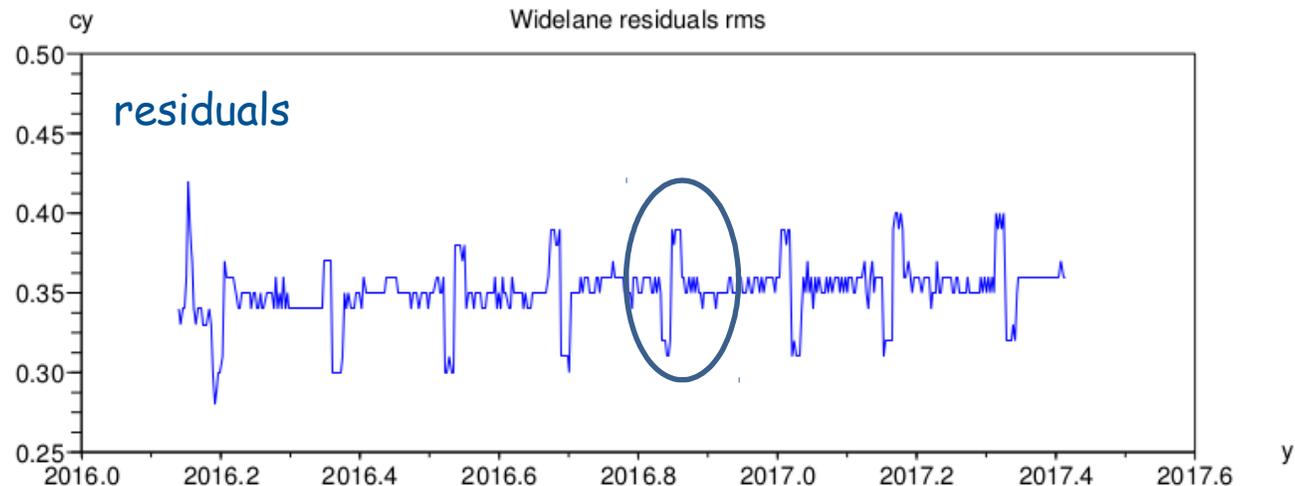
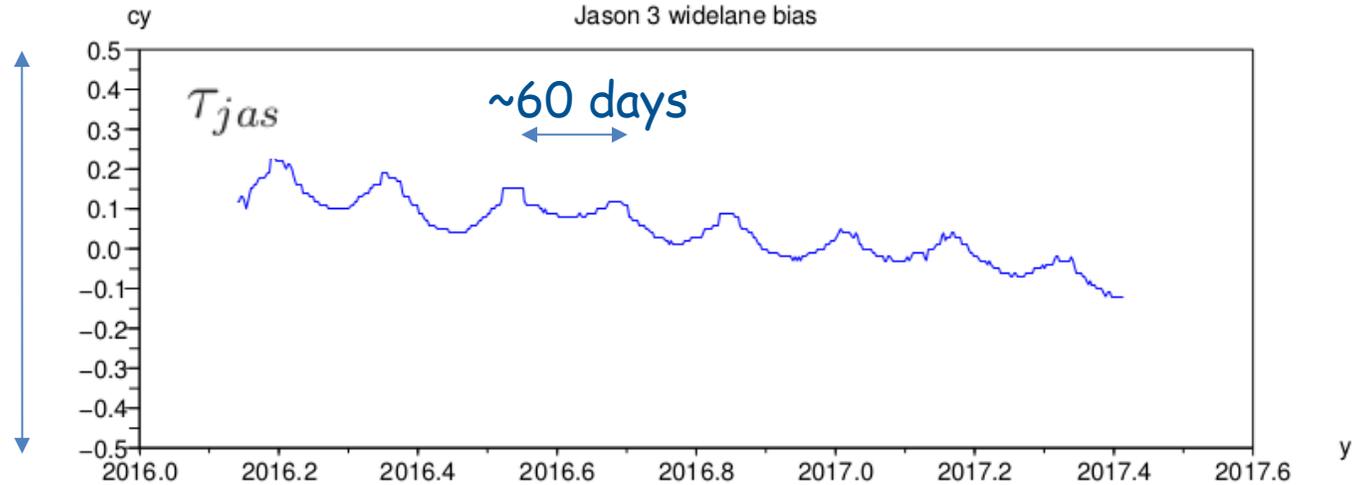
All passes are fixed

- no pass elimination

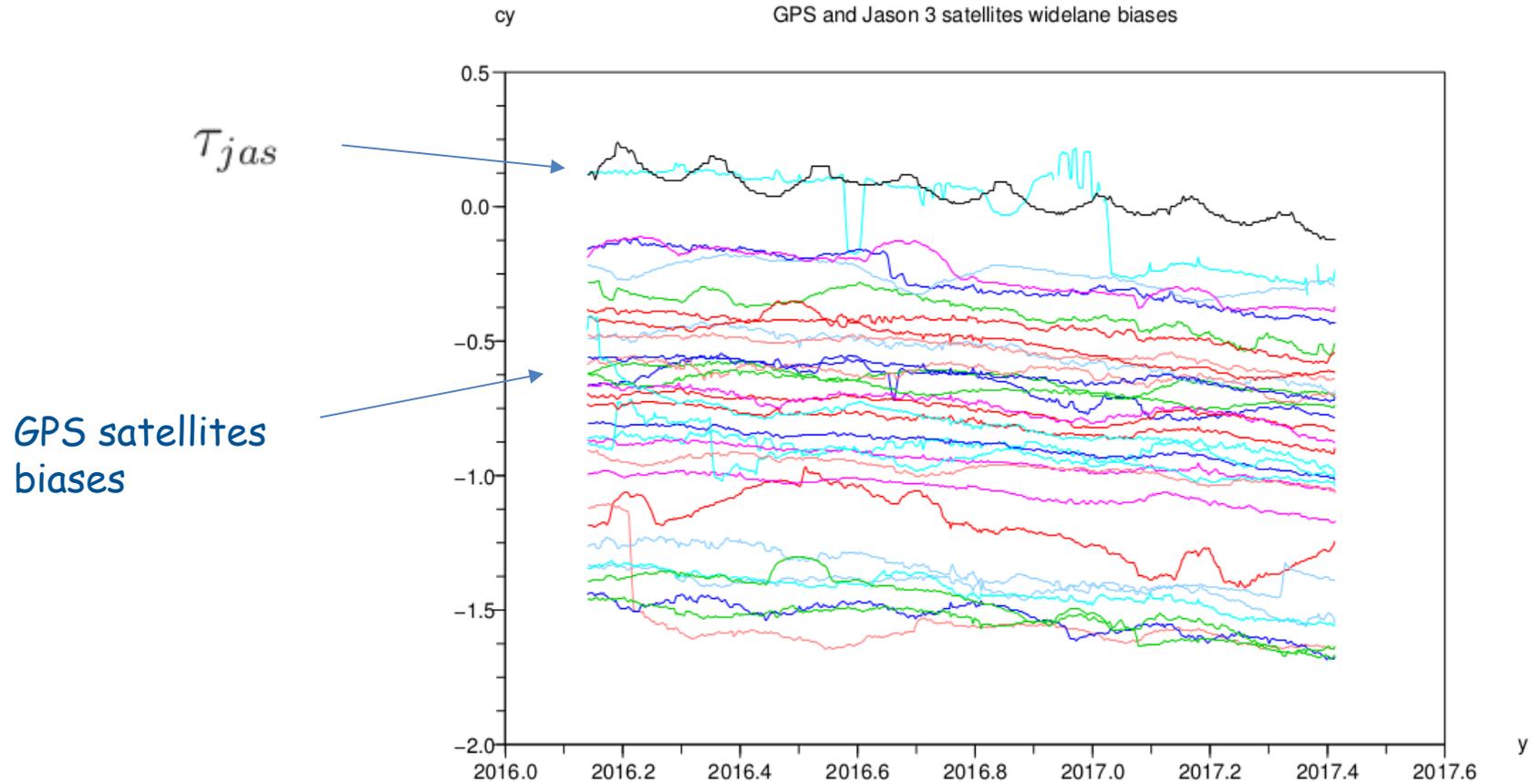
- $N_w - \tau_i + \tau_{jas}$

rounded to the closest integer

- small draconitic effects on  $\tau_{jas}$
- attitude effects on residuals rms



# widelane biases drift ? The drift observed in $\tau_{jas}$ is probably due to the GRG solution



→ Robust widelane ambiguity fixing, independent for each pass

## Second ambiguity fixing

Global fixing on a reduced problem :  
 ambiguity per pass and receiver clock bias per epoch  
 the orbit is fixed (the floating ambiguities orbit precision is sufficient)

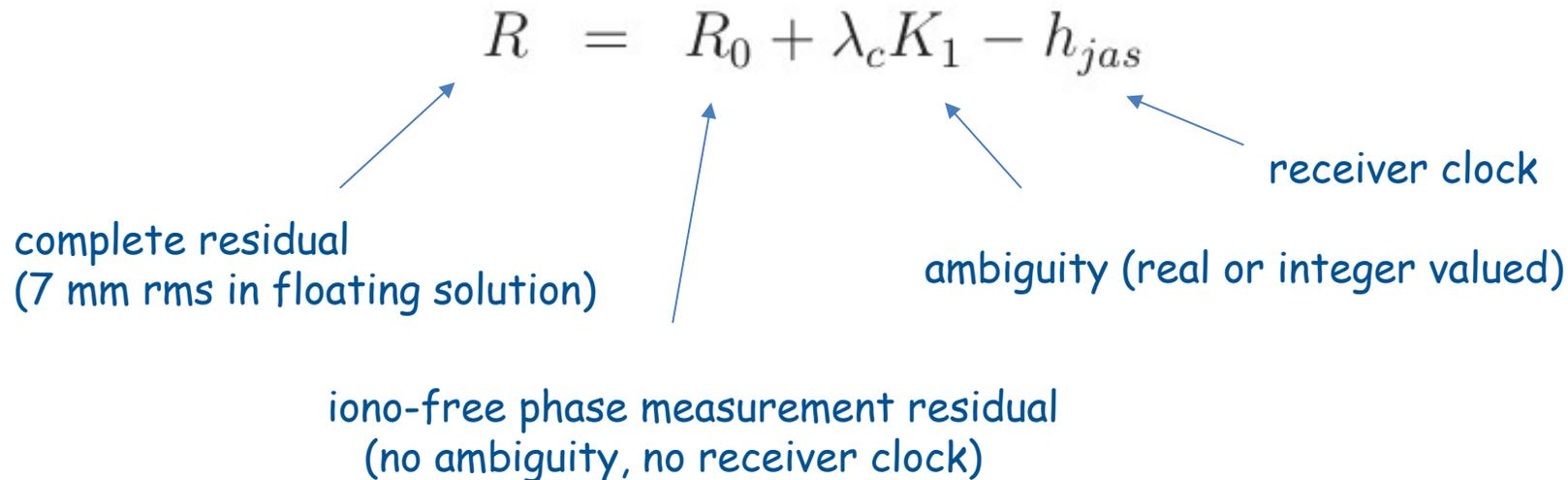
$$R = R_0 + \lambda_c K_1 - h_{jas}$$

complete residual  
(7 mm rms in floating solution)

iono-free phase measurement residual  
(no ambiguity, no receiver clock)

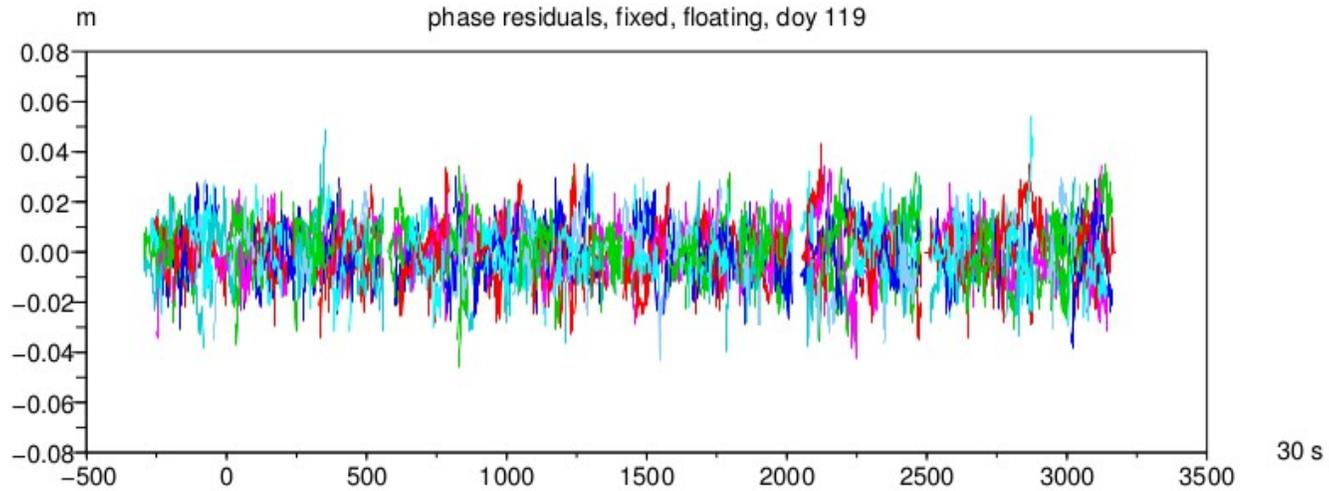
ambiguity (real or integer valued)

receiver clock

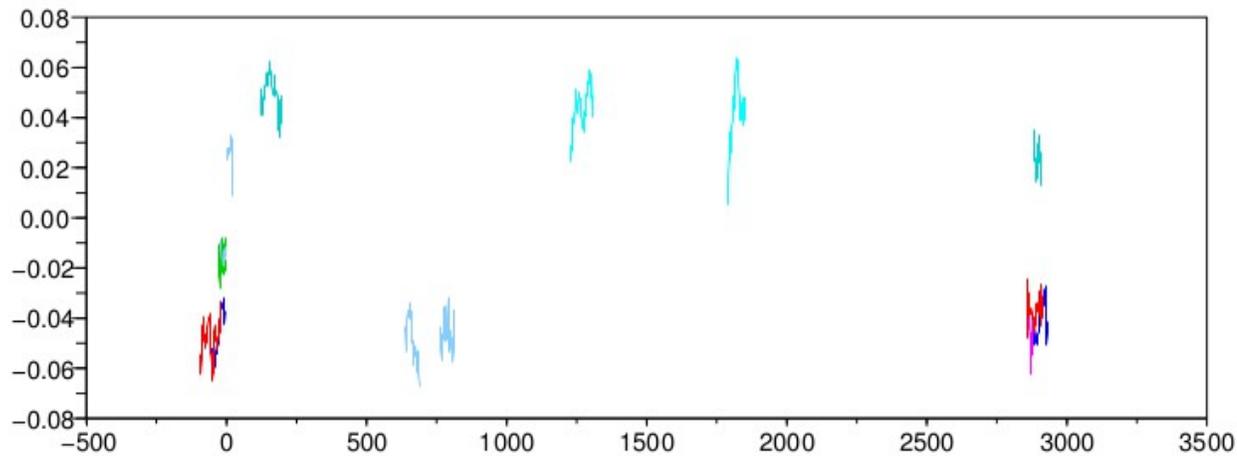


What are the results when  $K_1$  is rounded to the closest integer ?

# Residuals after ambiguity fixing



Fixed



Floating

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## New orbits

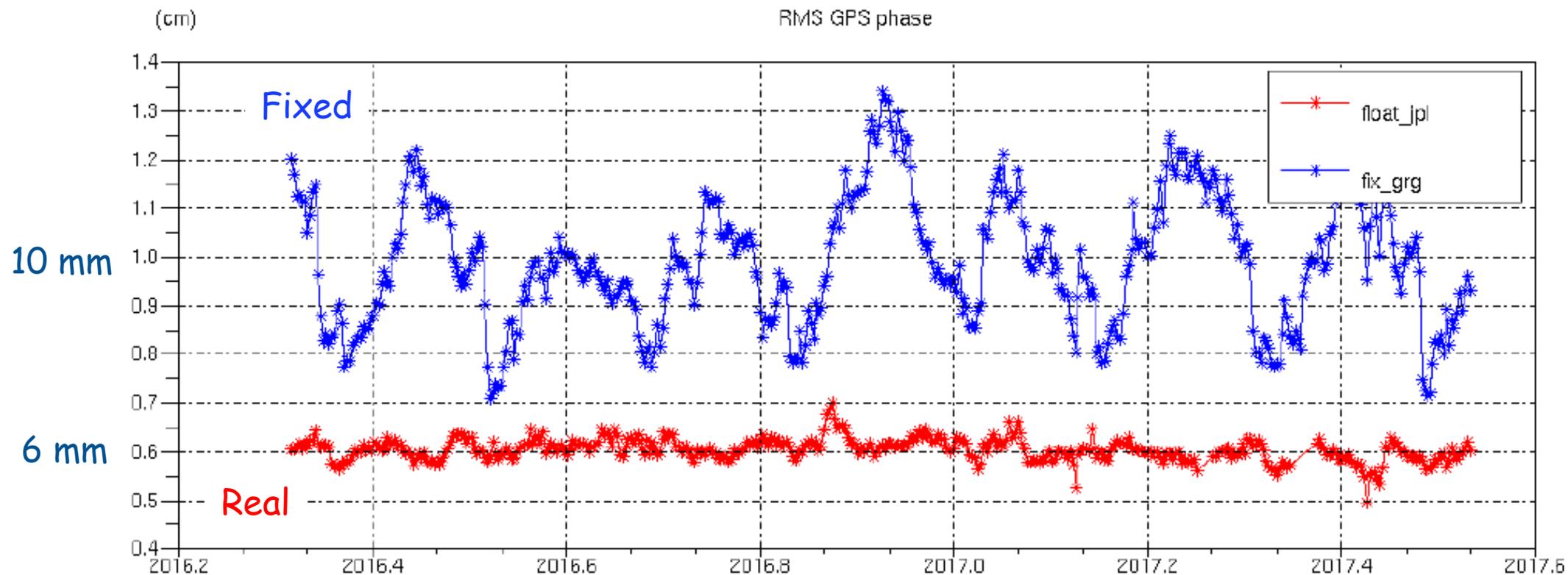
GDR-F standards (geocentre, tides...)

Effect of the normal bias

Floating or fixed ambiguities

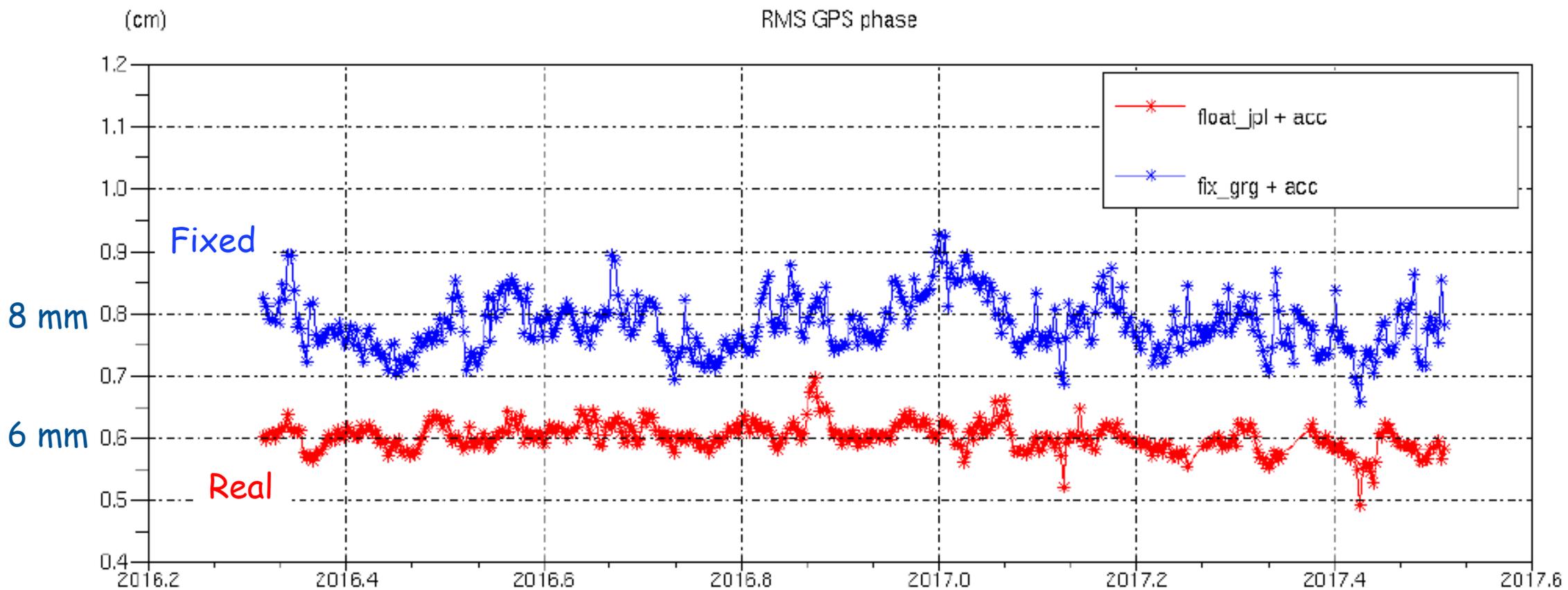
SLR validations

# Effect of fixing ambiguities



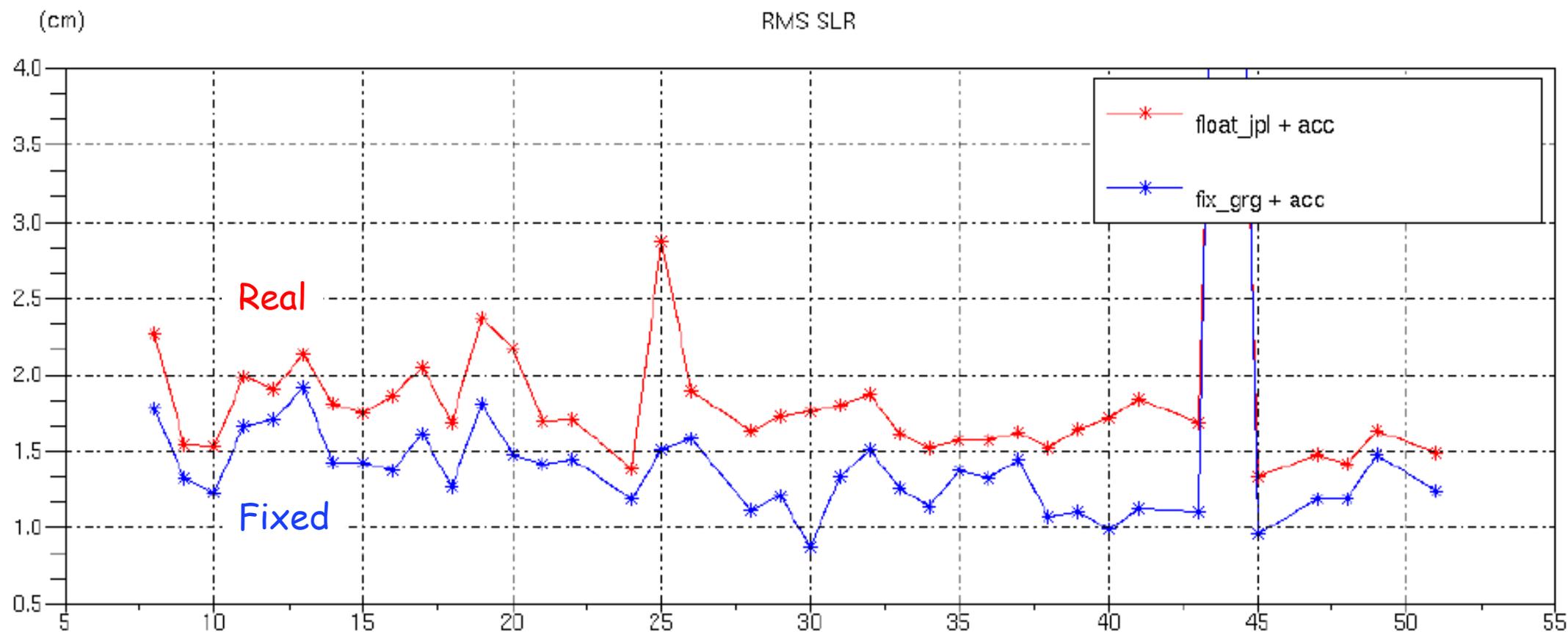
The fixed solutions rms values have important fluctuations, correlated with beta angle  
(no normal acceleration bias adjusted)

# Effect of fixing ambiguities and adjusting normal bias



The beta angle dependency is minimized for the fixed ambiguities solutions  
(normal acceleration bias adjusted)

# SLR residuals, all stations, all elevations



Improvements mainly due to the along track bias removal