

# Towards a spectral error budget of Nadir Altimetric missions



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OST/ST 2014

October 27-31, 2014  
Konstanz, Germany

# Overview

- **Altimetry** system provides more and more precise data.
- But, as every remote sensing system, it is affected by **errors**, more or less known and described.
- This presentation is dedicated to **altimetry users** and presents a state of art of the work performed to deliver, jointly to the altimetry products, an estimation of their associated error.
- A series of metrics and diagnoses already enable to constitute an error budget, which can be confronted with the mission goals and specifications.
- But, depending on the applications, **the errors at different spatial and temporal scales are not the same.**
- With the new era of wide swath altimetry, we need to **decline the error budget for various temporal and/or spatial scales.**
- This presentation focuses on the way this new metrics are getting prepared.

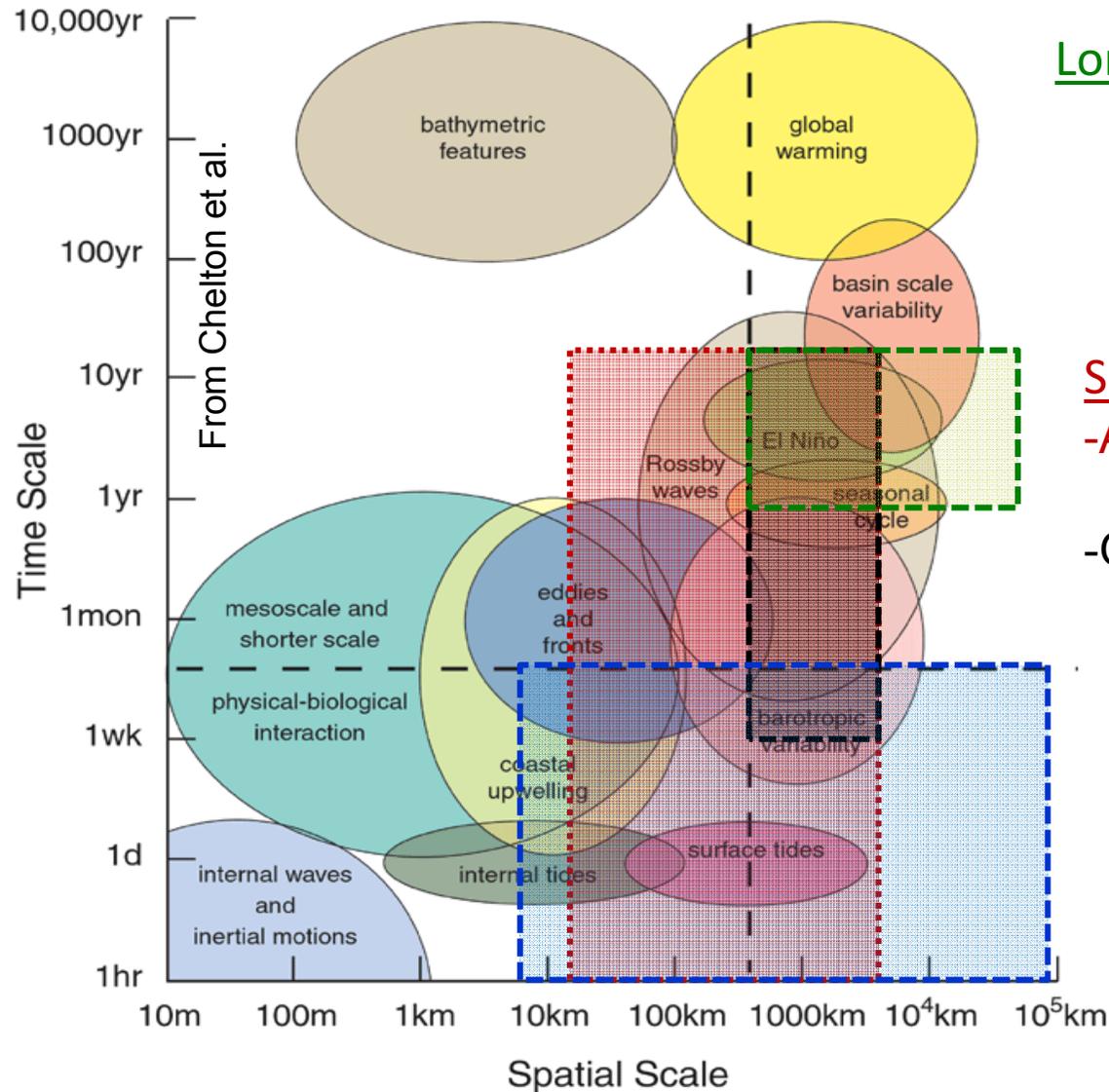
# Overview

For this study, data used are along track Jason-2 GDR-D Level-2 products.

This presentation is splitted into 3 parts:

1. Background and presentation of the problem
2. Example of metrics and analysis of the spectral content
3. Taking into account the spatial/temporal dependency: notion of enveloppes

# Background



## Long term trend analysis:

1Hz along track data  
annual cycle removed

*Ex: Ablain et al. Poster*

## Spectral analysis on:

-Along track 1Hz

*Ex: Ubelman et al. OSTST 2013*

-Gridded maps (280km)

*Ex: Pujol et al. Next talk*

## Crossover statistics:

along track data

1Hz (7km)

below 10 days

*Ex: Philipps et al. OSTST 2012*

# Background

- The specifications of the mission consists in integrated values over all frequencies available for all the corrections included in the SSH definition:

$$\text{SSH} = \text{Orbit} - \text{Range} - \text{Iono} - \text{Sea State Bias} - \text{Dry tropo} - \text{Wet tropo}$$

From Philipps et al. OSTST 2012

	Error budget	Error (<10 days)			GOAL
		OGDR	IGDR	GDR	
Parameters and corrections for raw sea surface height	Altimeter range	>1.6 - 1.7 cm			1.5 cm <sup>a,b,c</sup>
	Ionosphere	>1 cm / >0.2 cm			0.5 cm <sup>d,c</sup>
	Sea State Bias	>0.4 cm			1 cm
	Dry troposphere	0.4-0.7 cm	0.3-0.7 cm		0.7 cm
	Wet troposphere	>0.2 cm			1 cm
	Rms Orbit (radial component)	>3.7 cm	>1.7 cm	>1.0 cm	1.5 cm

2.25 cm<sup>2</sup>

0.25cm<sup>2</sup>

1cm<sup>2</sup>

0.49 cm<sup>2</sup>

1cm<sup>2</sup>

2.25 cm<sup>2</sup>

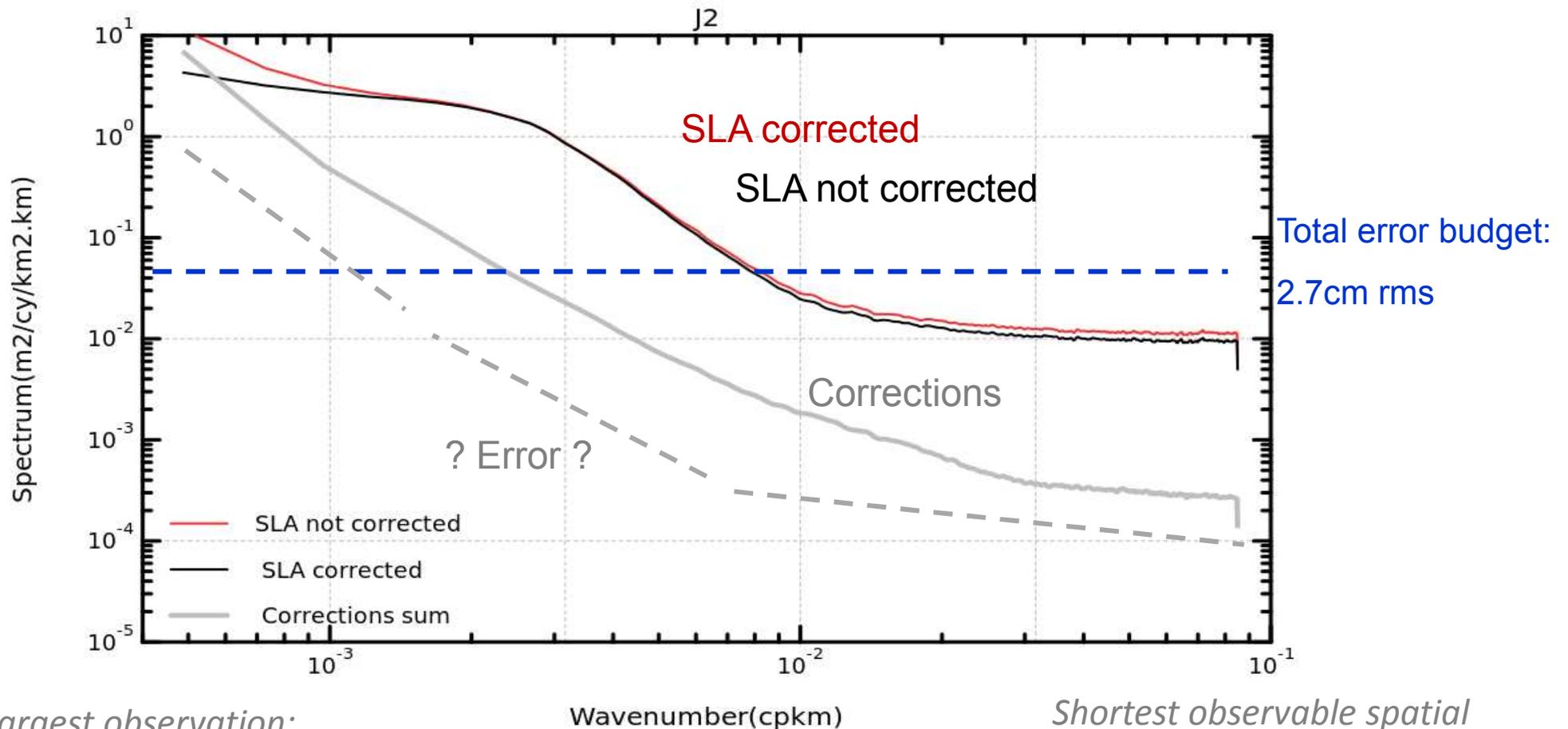
Philipps et al. Proposed an assesment of the specifications, relying on crossover statistics and adreses the **error below 10days.**

All errors are mixed even if we know they don't affect equally the same wavelengths.

2.7cm ← 7.24cm<sup>2</sup>

# Method

- Compared to the Sea Level anomaly power spectrum, our aim is to decline the integrated figures of the specification for each frequency between.

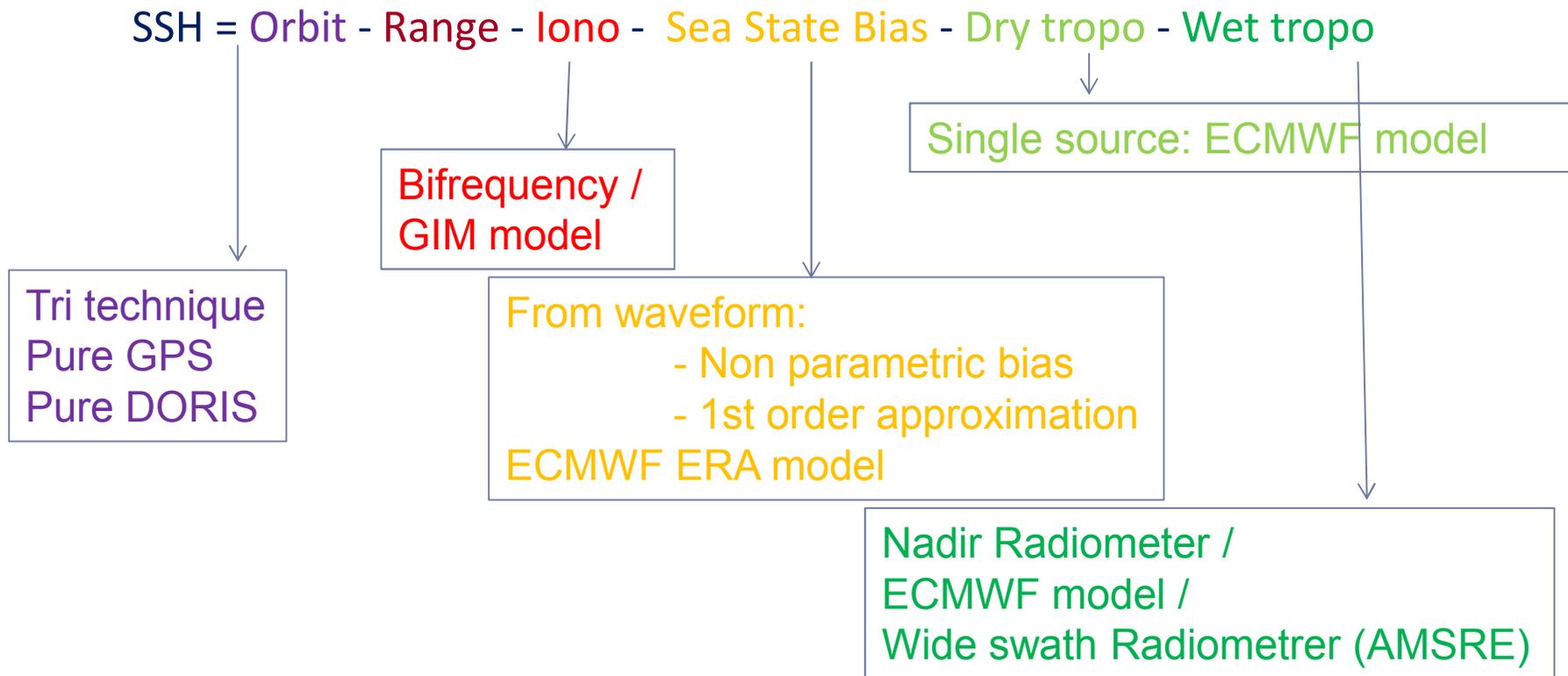


Largest observation:  
all the available latitudes 8 000km

Shortest observable spatial  
sampling: 14km / 1Hz sampling

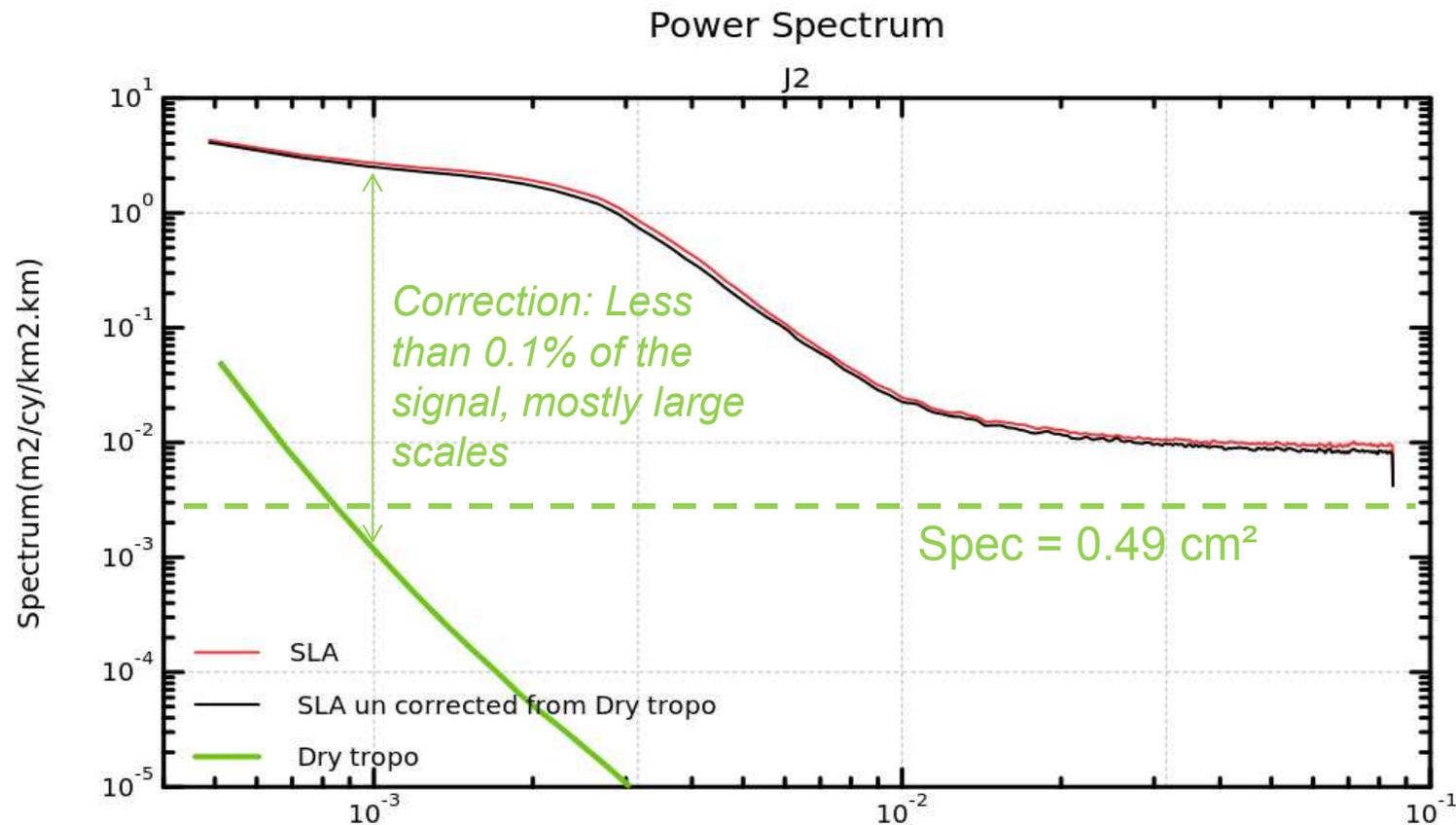
# Method

- In his presentation, Clement Ubelman (OSTST, 2013) initiated a break down of the errors spectral characterisation with a strong assumption of decorrelation of the correction with the corrected signal.
- Following his efforts we propose a complementary approach based on multiple sources of observation of a same geophysical content.



# Example of metrics and Analysis of the spectral content

Dry troposphere is a large scale effect, the only correction we have is an ECMWF model.

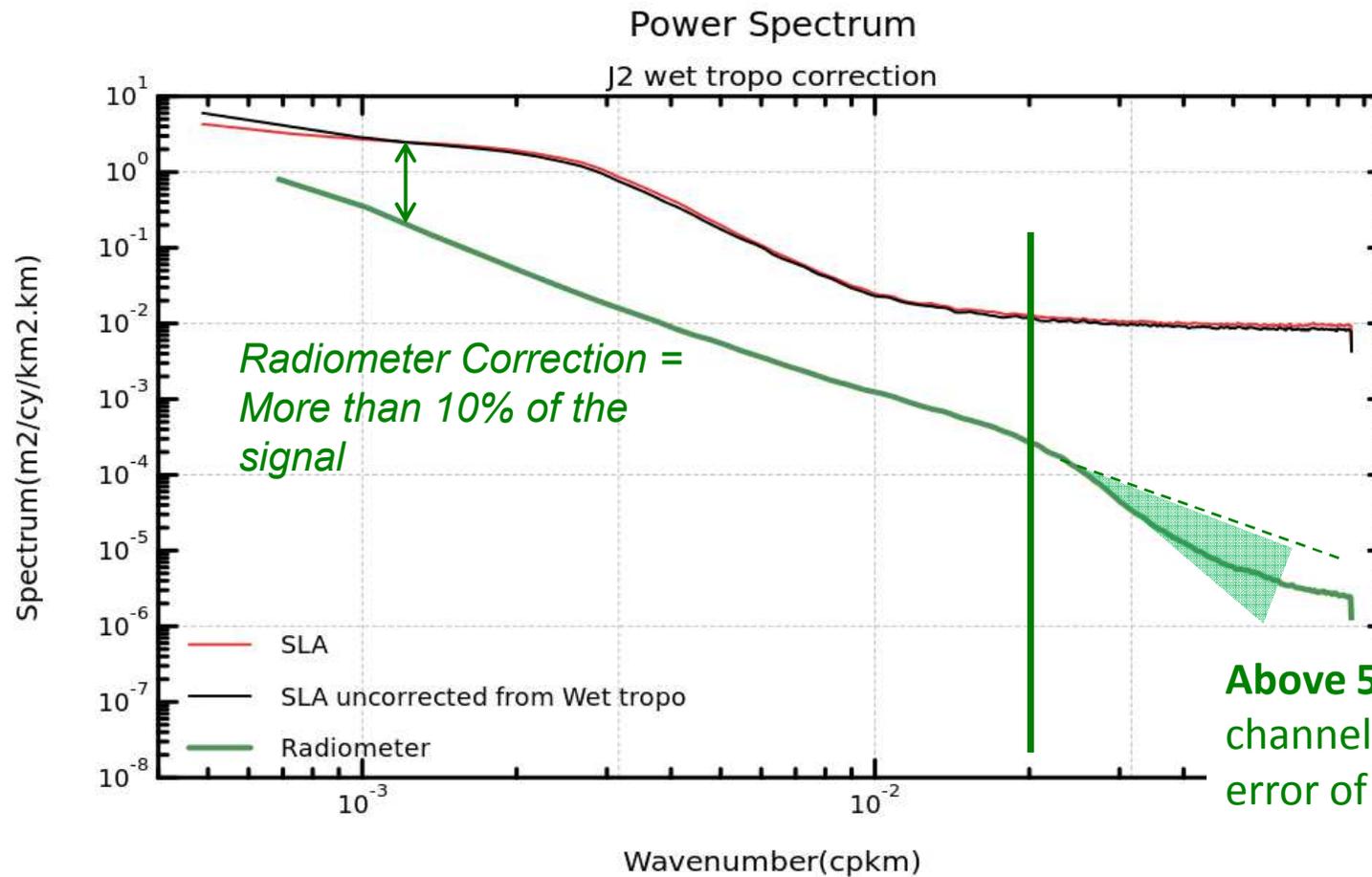


To characterise its error we can assume that it is below the correction itself (otherwise better not correct for it!).

The correction itself can be considered as an upper bound of its own error

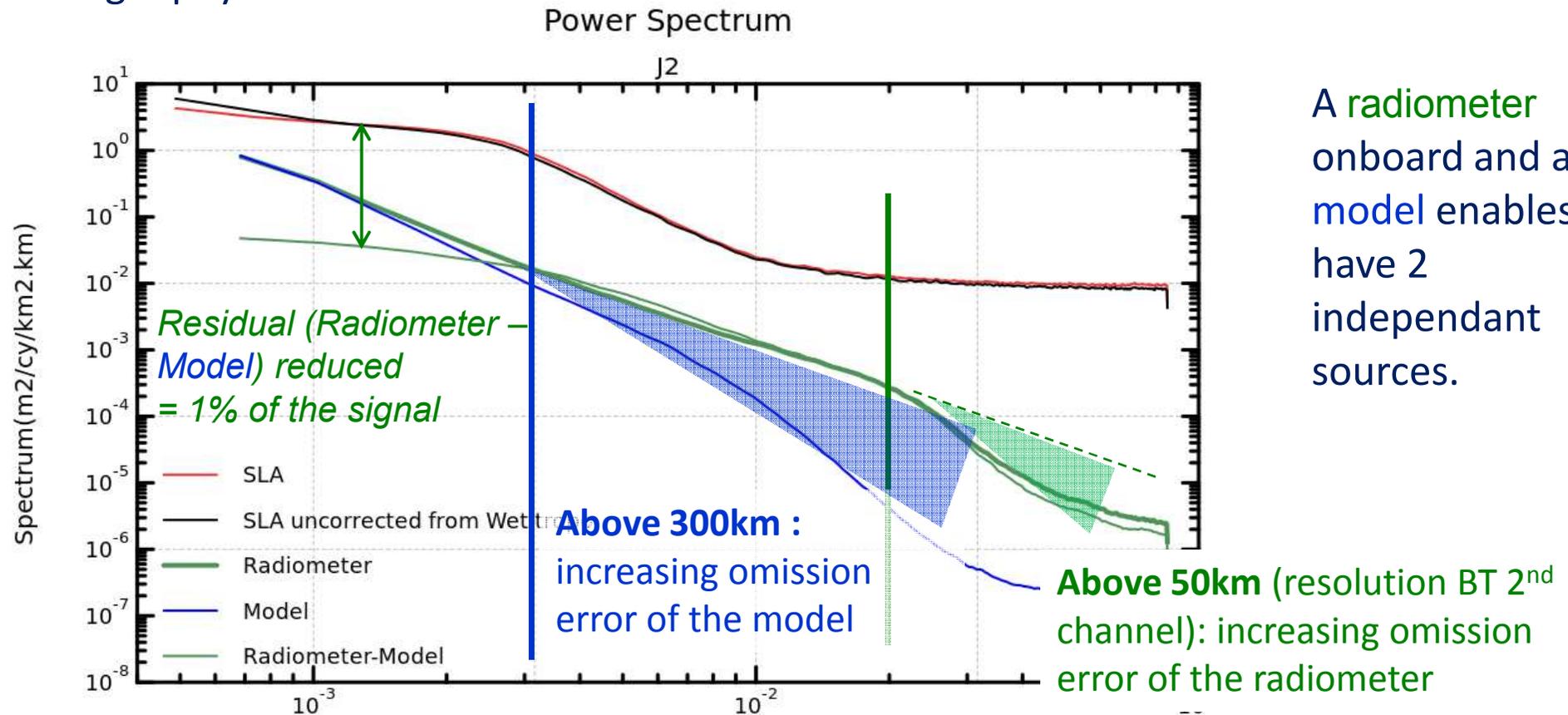
# Example of metrics and Analysis of the spectral content

**Wet tropospheric correction** is very critical signal because its signature is very close to the ocean geophysical content.



# Example of metrics and Analysis of the spectral content

Wet tropospheric correction is very critical signal because its signature is very close to the ocean geophysics.

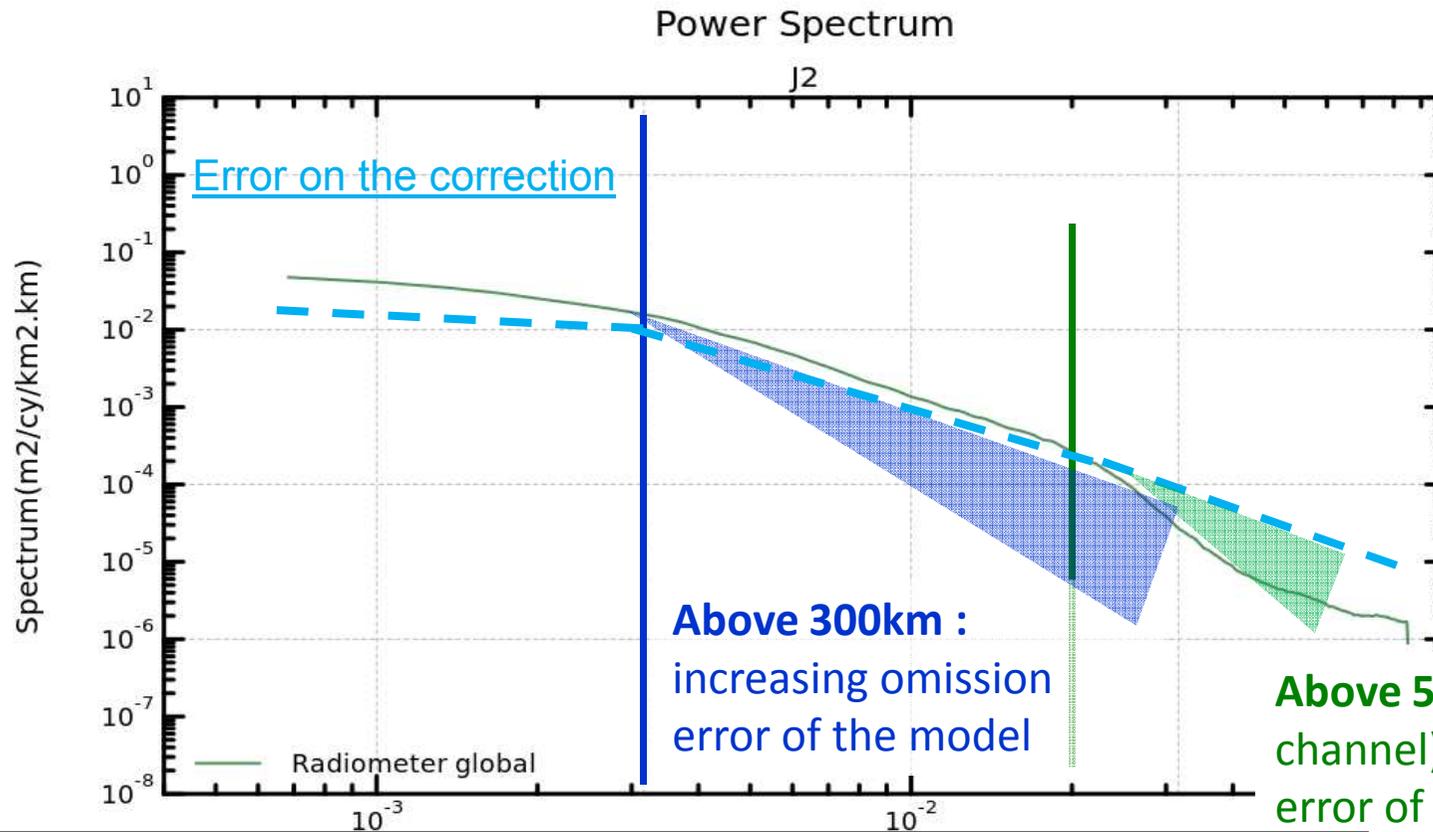


A radiometer onboard and a model enables to have 2 independant sources.

Multiple observations enable to refine a lot the error estimation if they are : **independant and consistent**

# Example of metrics and Analysis of the spectral content

**Wet tropospheric correction** is very critical signal because its signature is very close to the ocean geophysics.



A **radiometer** onboard and a **model** enables to have 2 independant sources.

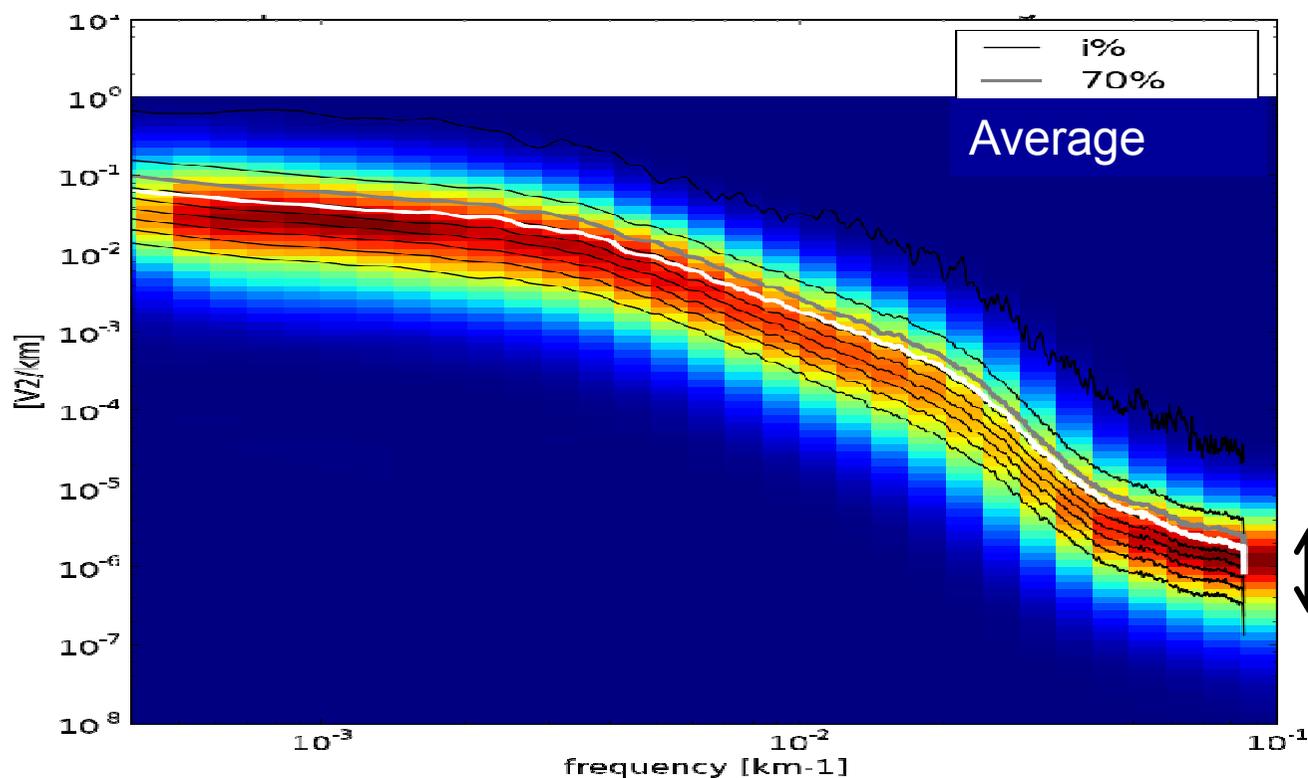
The upper bound of the error given by the signal itself is refined.

➔ Is this upperbound (average spectrum) relevant of all physical events????

# Taking into account the spatial/temporal dependency: notion of envelopes

- Distribution of individual spectra around the average (white)

Global average integrates many geophysical events.

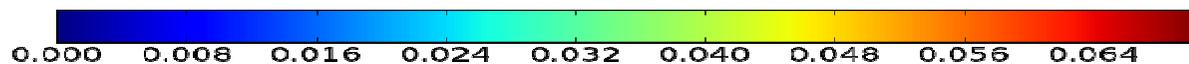


One single gaussian population around the average.

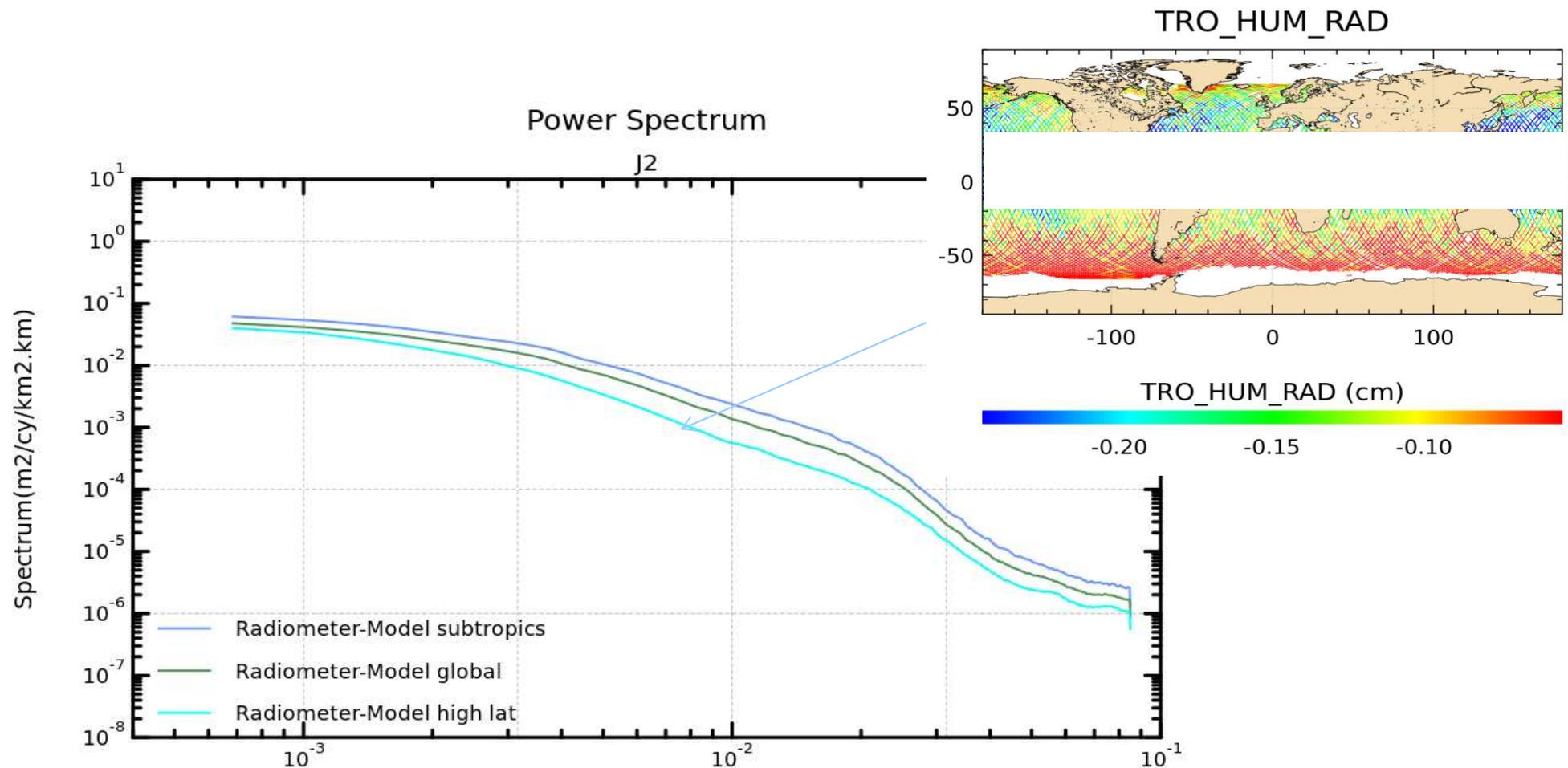
Few very energetic samples shift the average / mediane.

The energy of signal varies over more than one decade, depending on the geographic zone.

Number of individual spectra averaged per box



# Taking into account the spatial/temporal dependency: notion of envelopes



The envelope around the average enables to take into account the temporal/spatial variability of the signal observed.

Depending on the application, the upper/lower bound can be taken into account.

# Conclusion

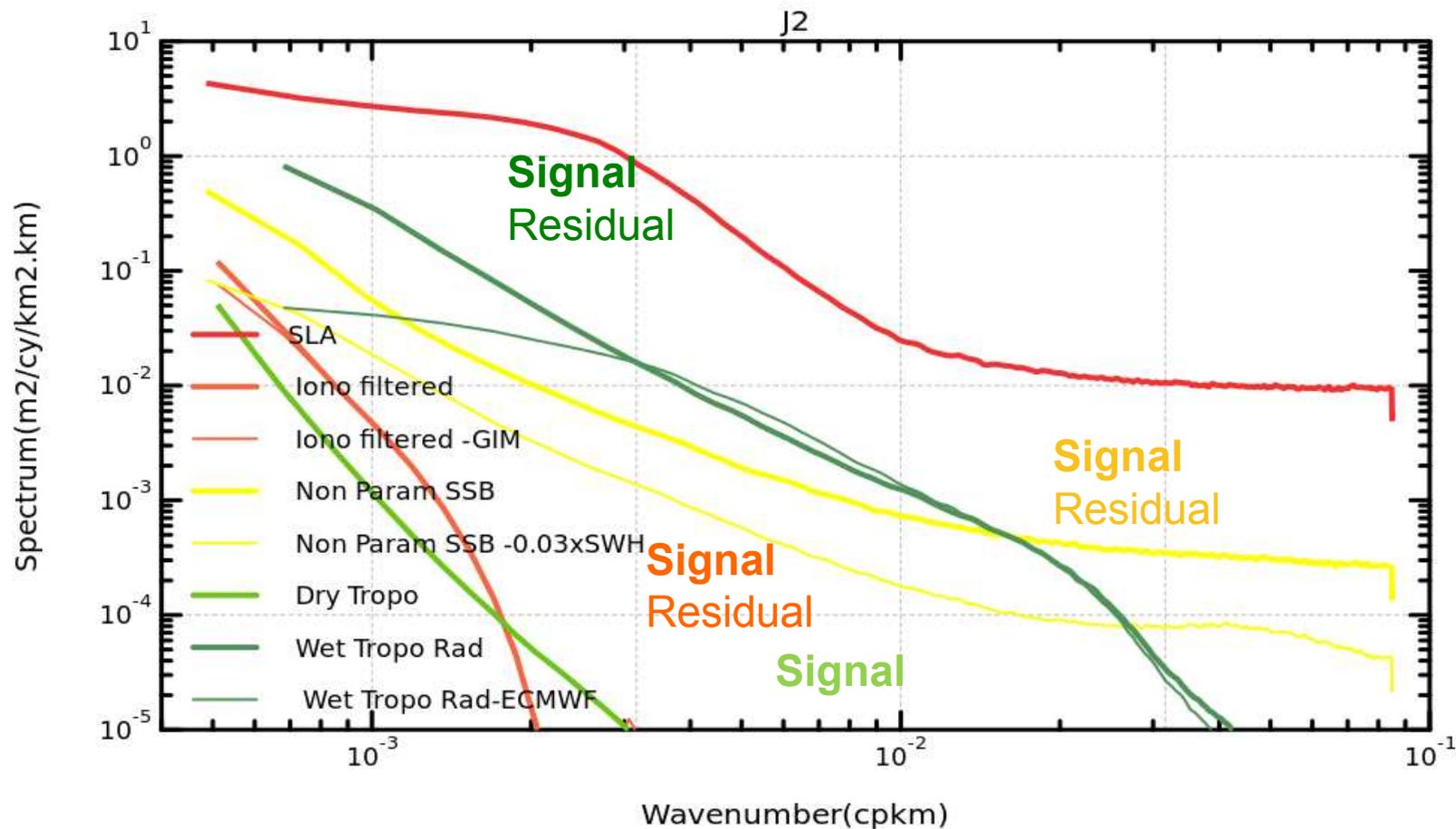
We showed that:

- The spectral analysis of the SLA corrections gives information on their distribution of energy relatively to the spatial scales
- The error of each correction is supposed to be below the correction itself. And it is an upper bound of what we look for.
- Multiple sources of a similar geophysics can be compared:
  - If they are fully independant, the error of the difference gives a more accurate upper bound
  - If they are not fully independant, the error of the difference is only an estimation, (may be underestimated) of the total error
- Considering the envelope around the average sprectrum enables to better take into account all the temporal/spatial situations

# Conclusion

- The work presented was derived for all correction.

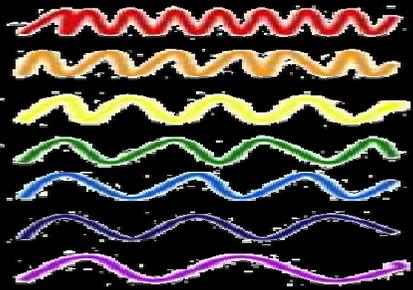
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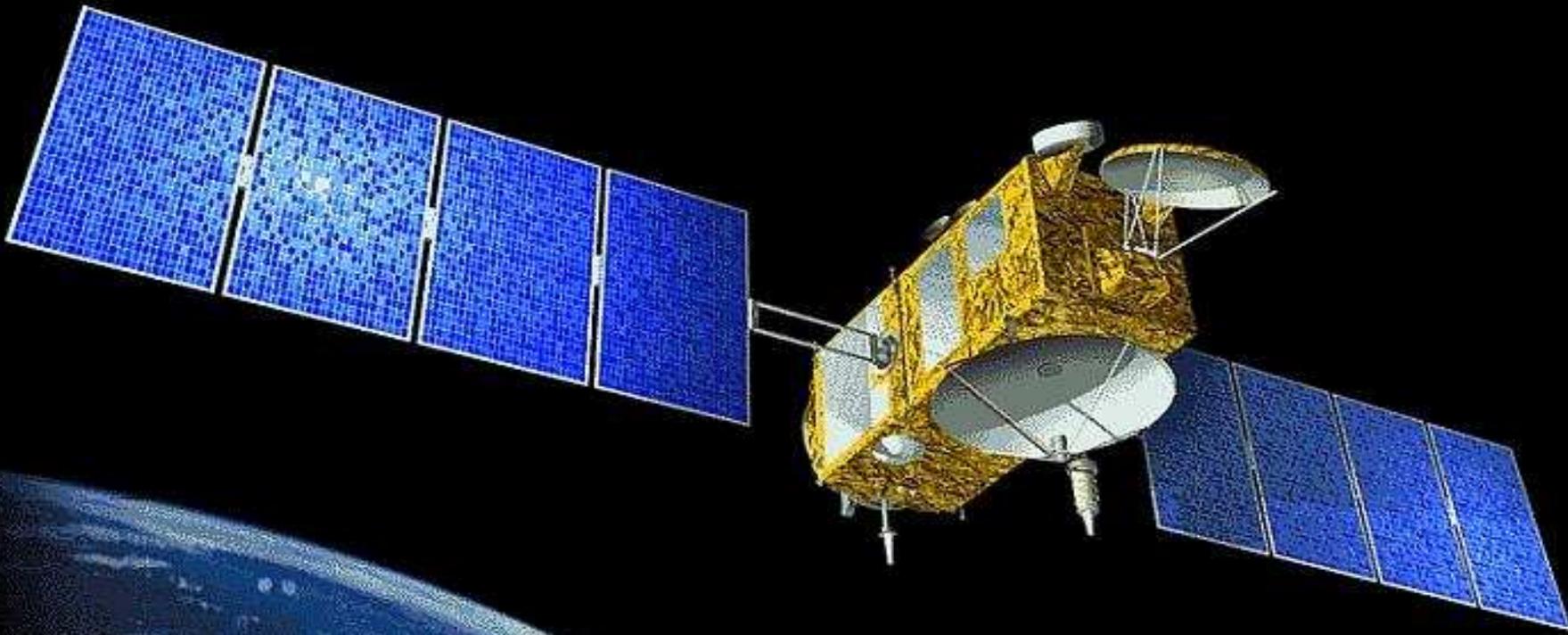
# Perspectives

- This work is on going...
- The method is complementary to other error estimation techniques and should be carried on jointly with them. For this:
  - Multiple observation system of a same correction must be carried on
  - The method can also be applied to other missions during tandem/not tandem phases

Discussions with the data users would be useful:  
What would they need?



Thank you for your  
attention

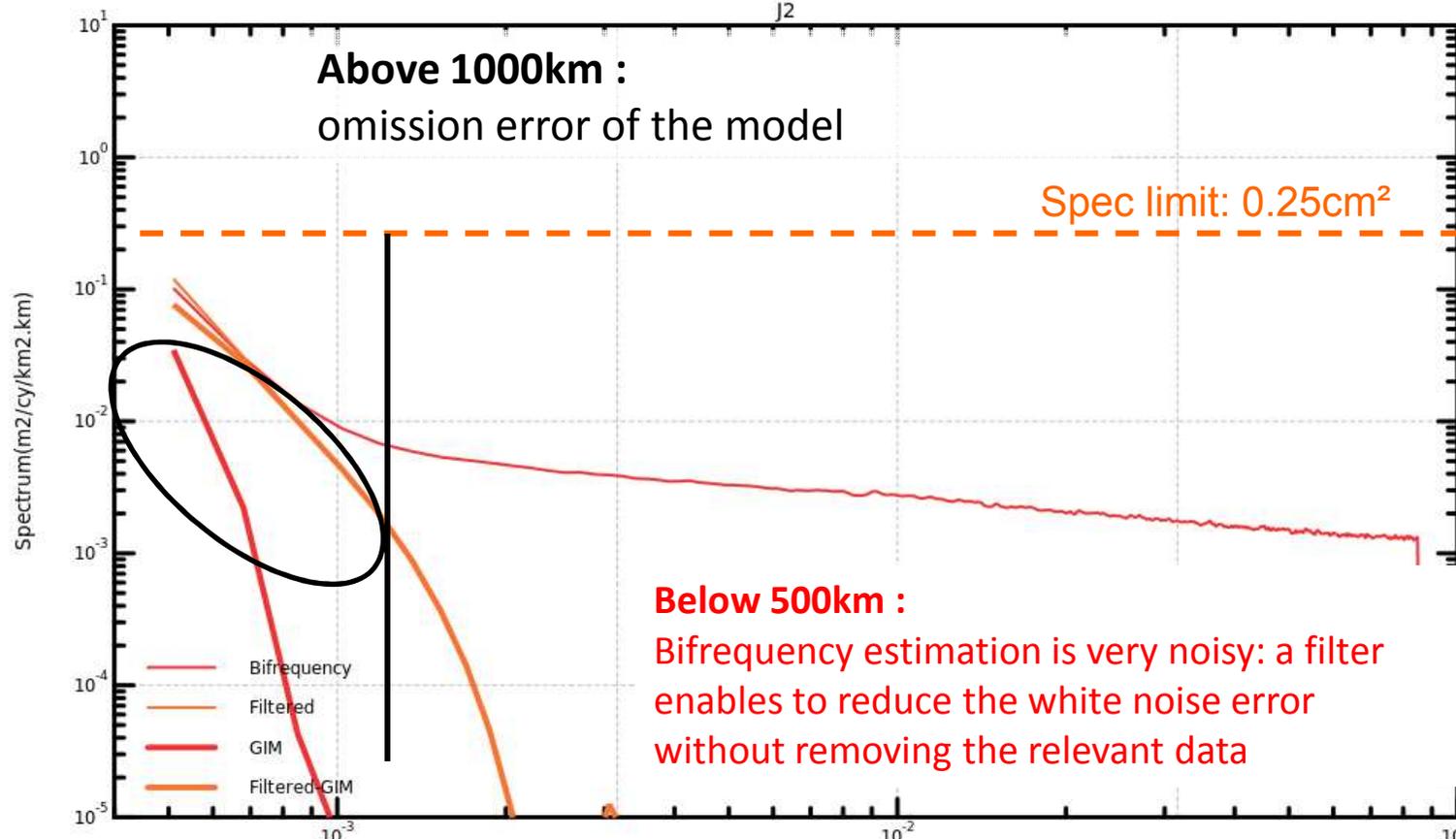


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# Example of metrics and Analysis of the spectral content

**Ionospheric correction** 's signature is weak in Ku (very weak in Ka) but the signature is very close to the ocean geophysics.

Iono correction Power Spectrum



**Above 1000km :**  
omission error of the model

A **bifrequency altimeter** onboard and a **model** enables to have 2 independent sources.

**Below 500km :**  
Bifrequency estimation is very noisy: a filter enables to reduce the white noise error without removing the relevant data

The model is very smooth and does not enable to reduce the error at these scales

# Method

- To do so, a break down on all the corrections is performed:

$$\text{SSH} = \text{Orbit} - \text{Range} - \text{Iono} - \text{Sea State Bias} - \text{Dry tropo} - \text{Wet tropo}$$

