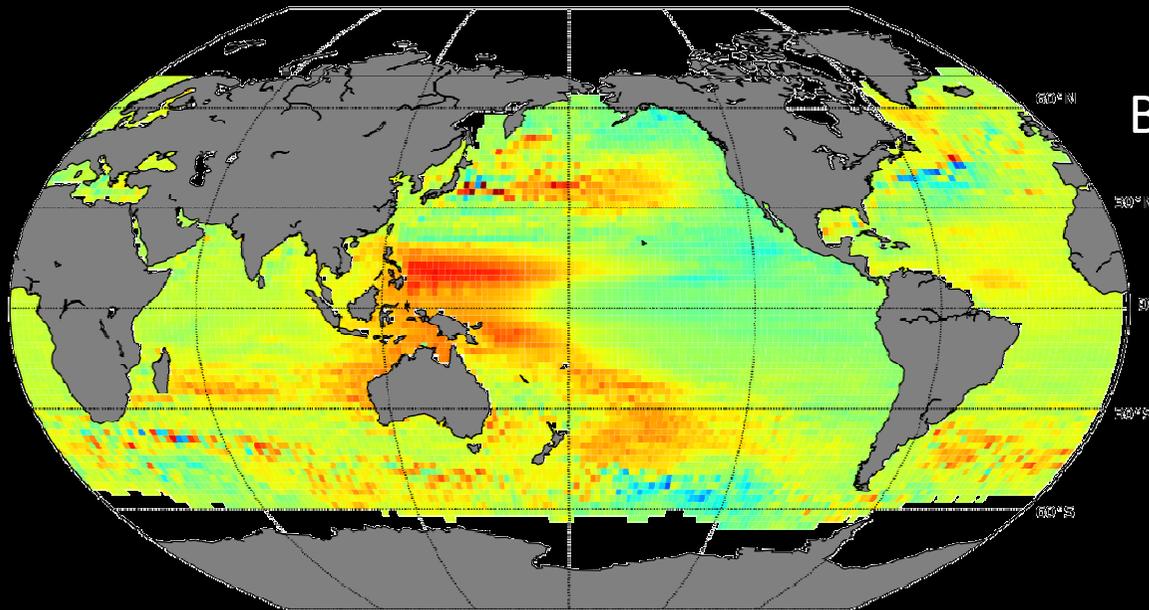


How reliable are regional sea level trends ?

?

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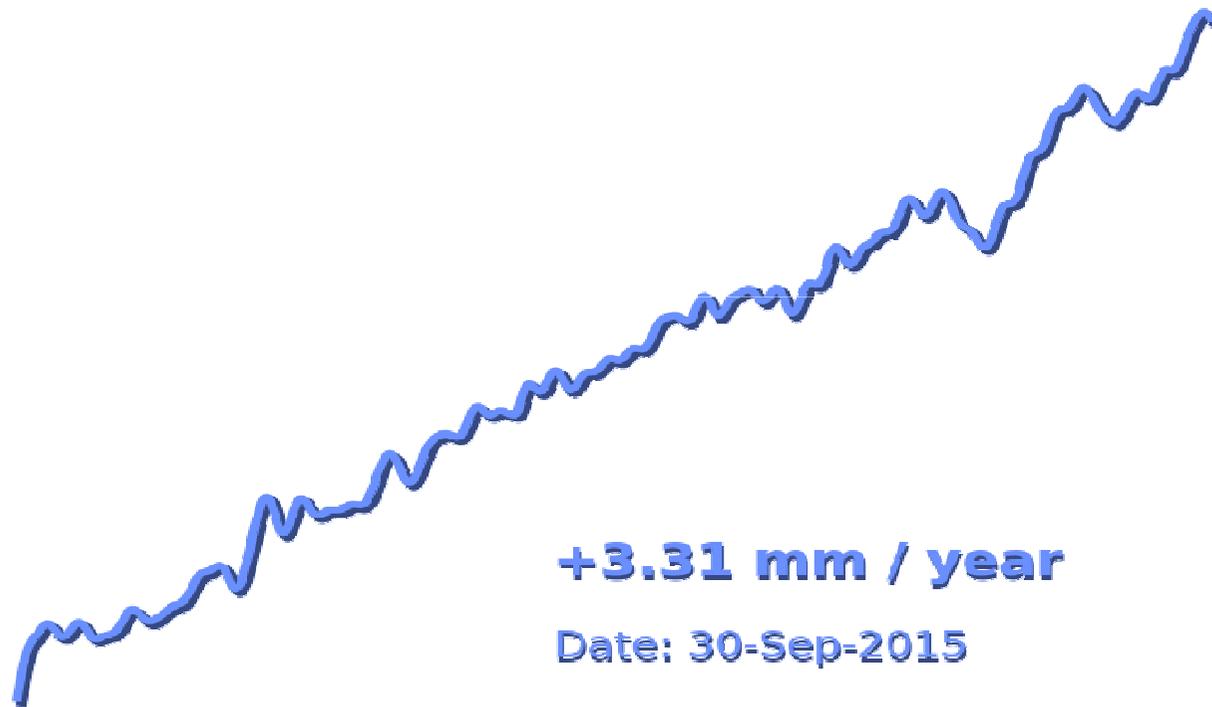


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Introduction

- MSL is an essential indicator of climate change,
- In particular, the trend draws much interest,



- What about associated uncertainties ?

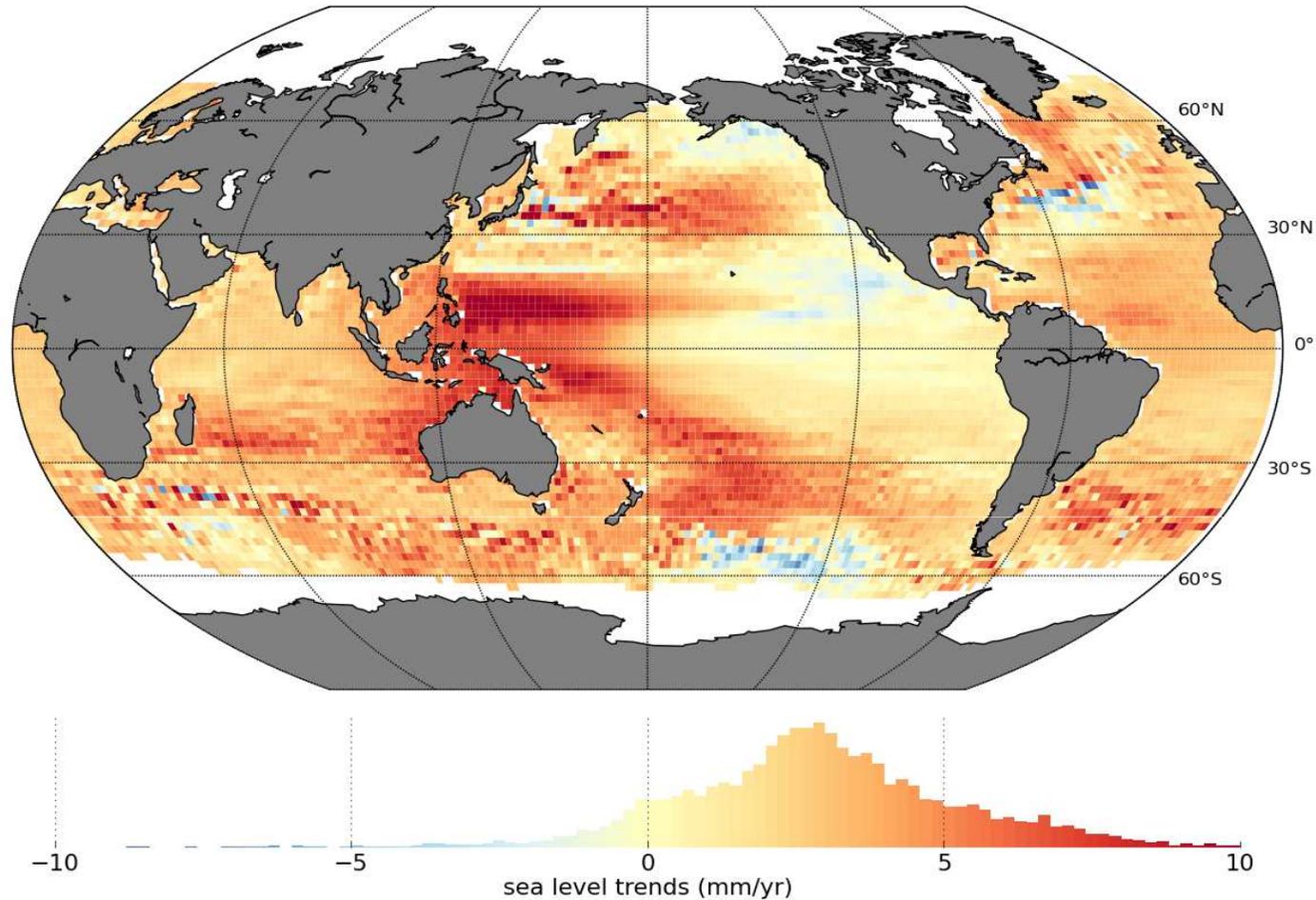
Uncertainties on global MSL

- Several reviews of uncertainty sources:
 - Ablain et al. 2009 & 2015

	Spatial scales	Temporal scales	Altimetry errors	User requirements	1993 to 2008
R Dyna	Global MSL	Long-term evolution (> 10 years)	< 0.5 mm year ⁻¹	0.3 mm year ⁻¹	
		Interannual signals (< 5 years)	< 2 mm over 1 year	0.5 mm over 1 year	
	Regional MSL	Annual signals	< 1 mm	Not defined	
		Long-term evolution (> 10 years)	< 3 mm year ⁻¹	1 mm year ⁻¹	
Total		Annual signals	< 1 cm	Not defined	1993 to 2008 at 90% confidence level

- Among others (Henry et al., Couhert et al., Legeais et al., ...)
- Results in **0.5 mm/yr** on GMSL, higher on RMSL

Objectives



- What are the uncertainties at each grid point ?
- Can we estimate a map of uncertainties ?

Mathematical approach

- At each grid point, we solve for the linear system

$$Y = XA + E$$

- The solution is given by

$$A = \left[X^T C^{-1} X \right]^{-1} \left[X^T C^{-1} Y \right]$$

- And the variance-covariance of model parameters

$$\Omega = \left[X^T C^{-1} X \right]^{-1}$$

Allows the determination of model parameter uncertainties

Mathematical approach

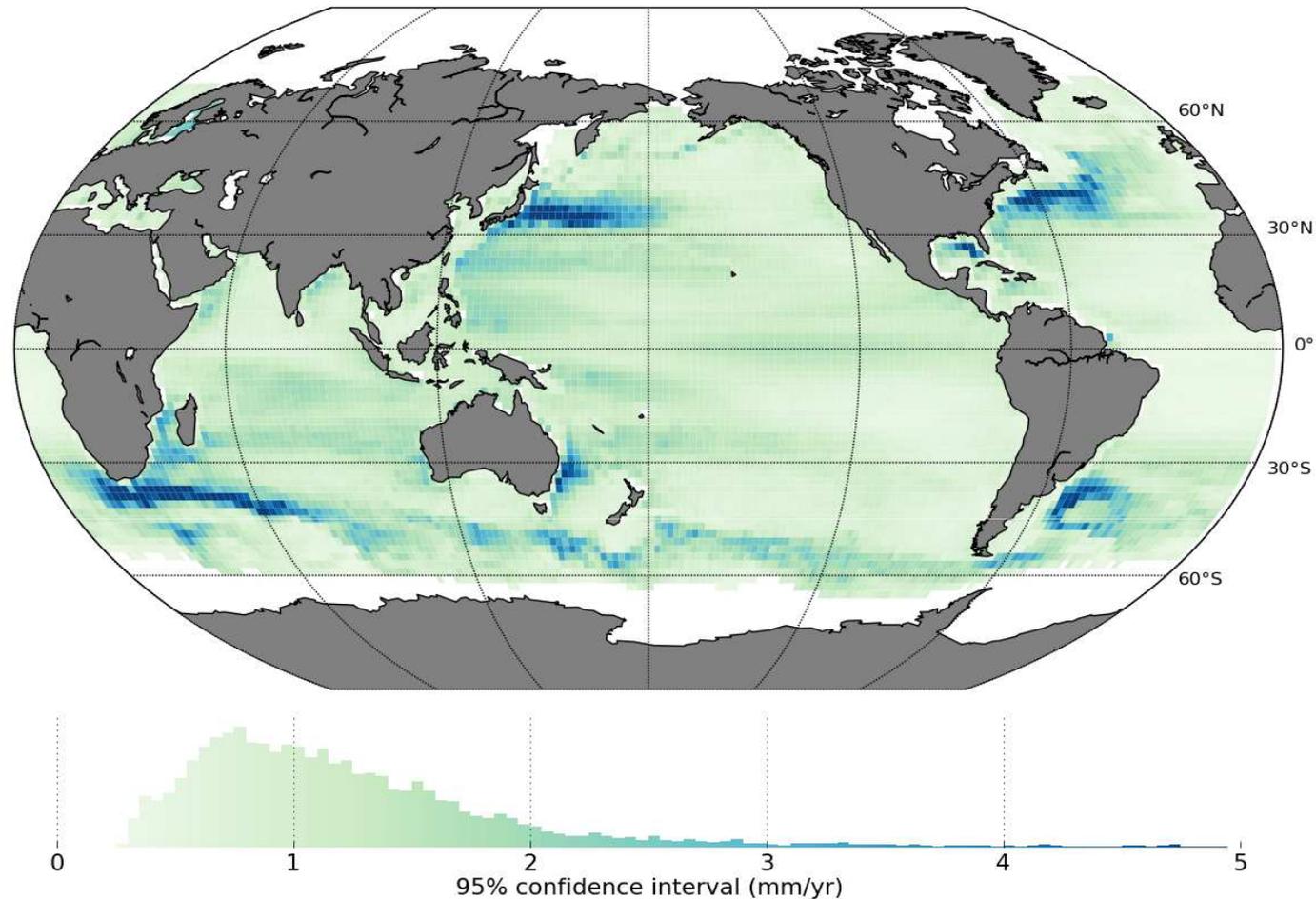
- C is the variance-covariance of the errors,
- a common simplification is to use

$$C = \sigma I_n$$

Which is simply the OLS solution (independent and identically distributed errors)

- Here, we populate the C matrix using reasonable assumptions on the error structure (GLS solution) and estimate 95% c.i. on trends

A useful reference: OLS



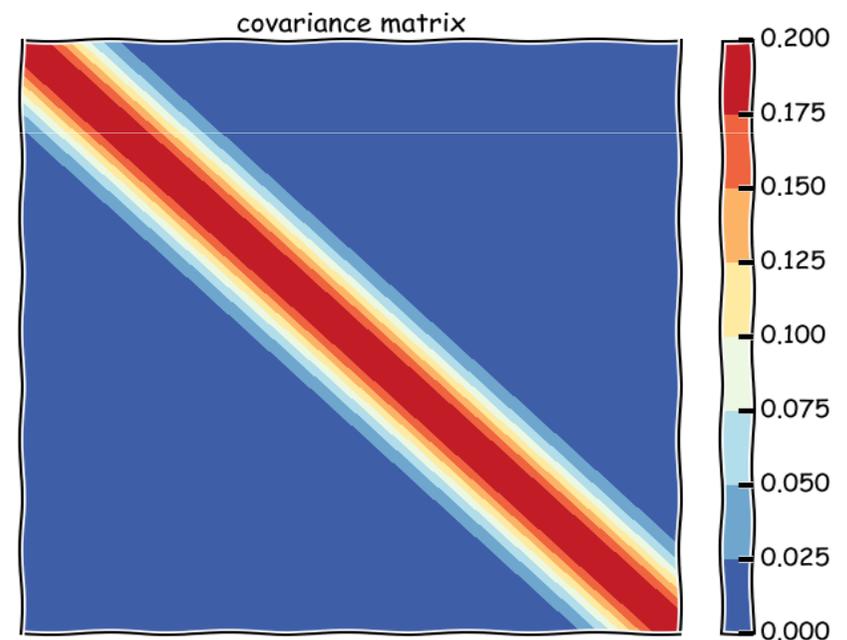
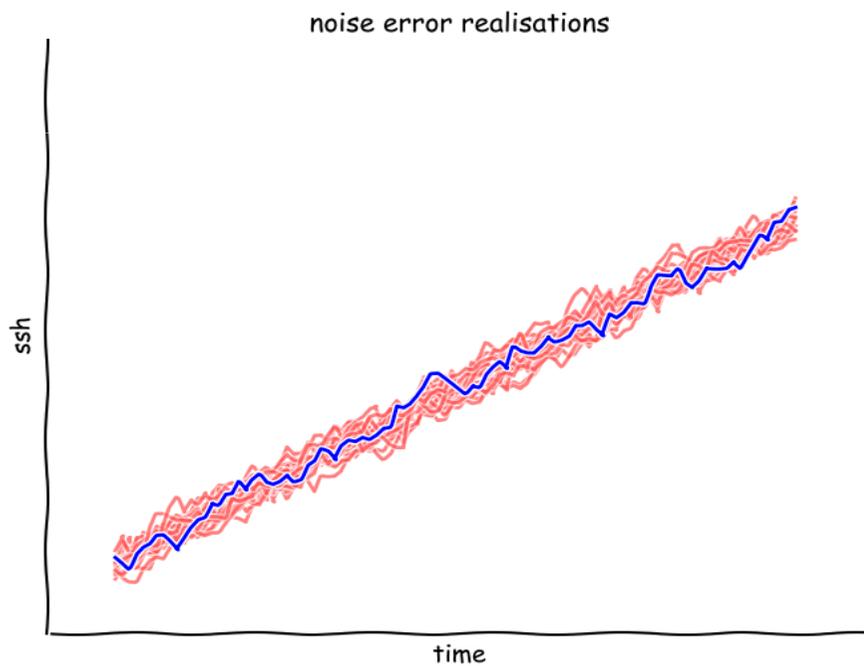
- Signature of ocean variability
- Uncertainties generally ranging from **0.5 to 1.5 mm/yr**

Error covariance model

- 3 error models are used:
 - noises,
 - biases,
 - drifts.
- At each grid cell, the total covariance is a sum of these « elementary » covariances.
- Based on a priori assumptions on errors at this point.

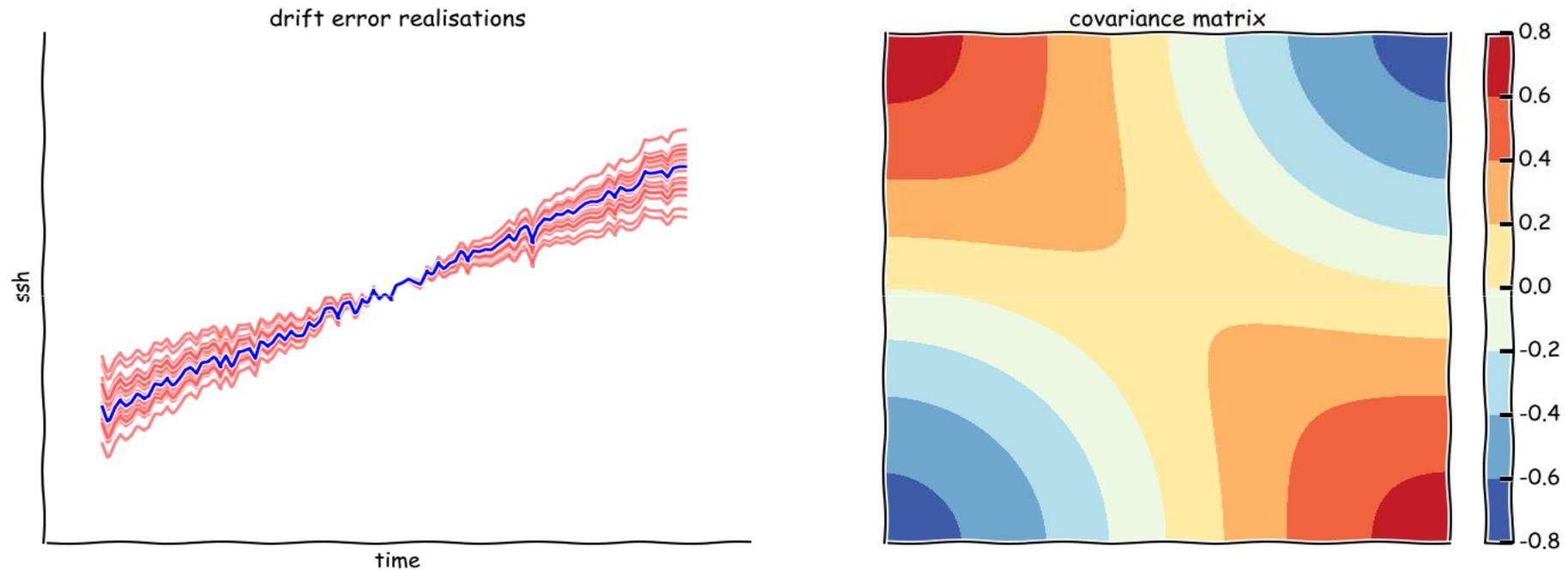
Noise

- Accounts for high frequency errors in altimeter data
 - With autocorrelation,
 - Without heteroskedasticity,



Drifts

- Accounts for uncertainties on long-term stability of the record

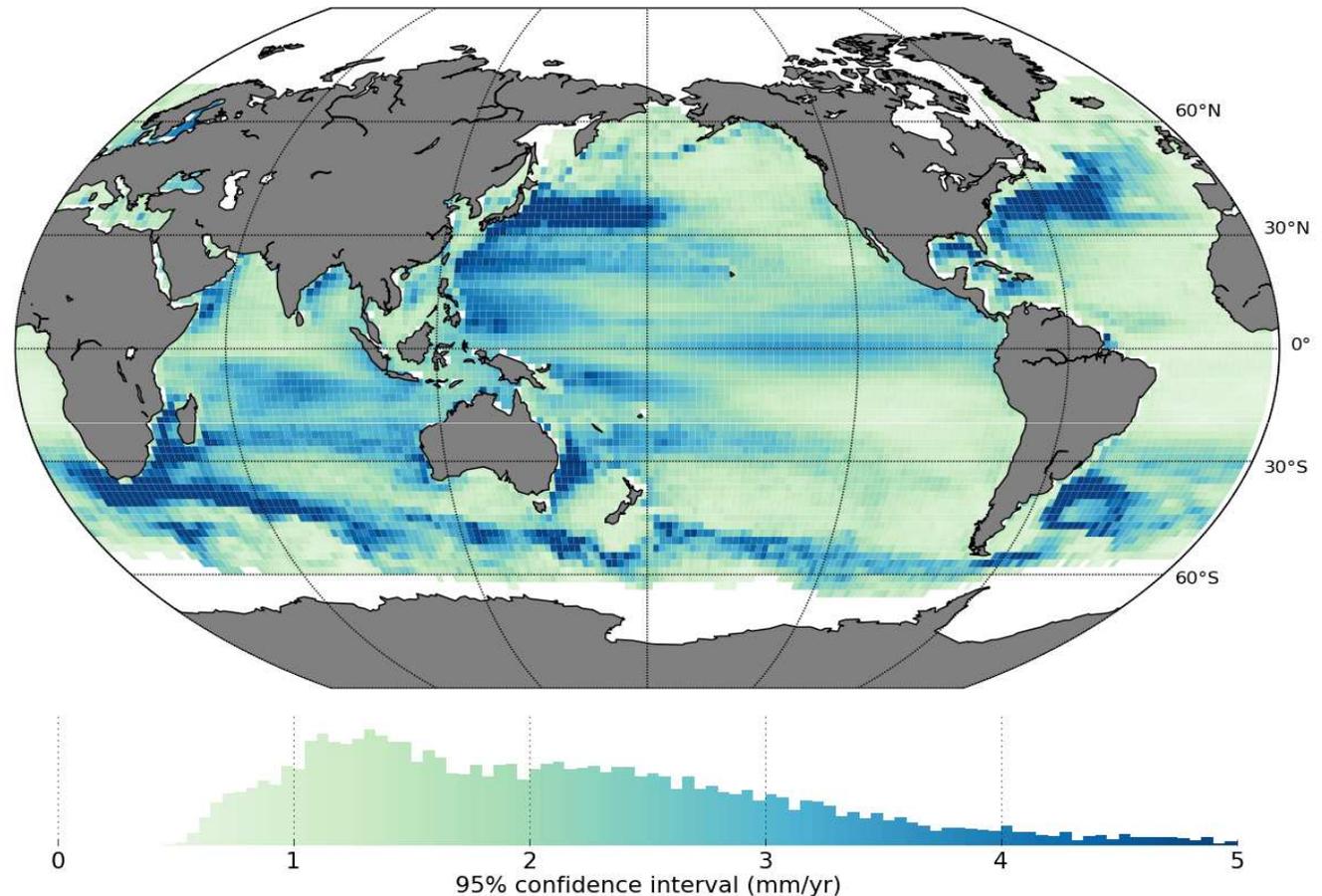


- Mainly due to orbits (Couhert *et al.*, 2015)
- And radiometer drifts (Legeais *et al.*, 2014)

Accounting for system errors

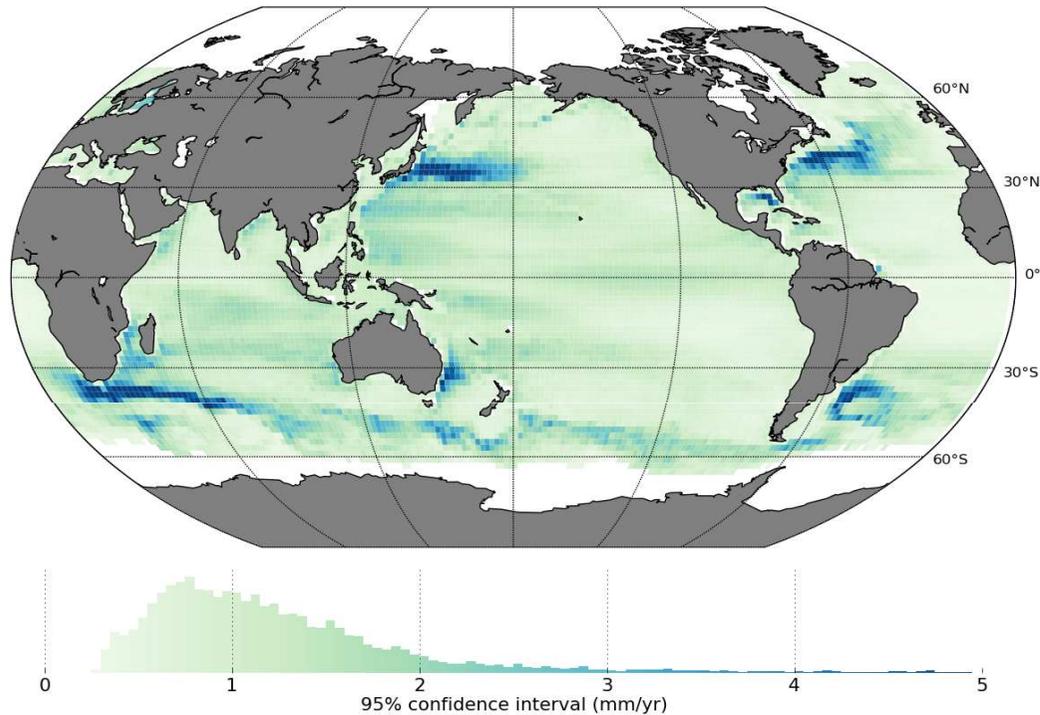
Assumptions:

- Orbit drift (1 mm/yr),
- Tropo drift (0 to 2 mm/yr, latitude dependent),
- biases errors between missions,
- High frequency correlated noise (2 months)

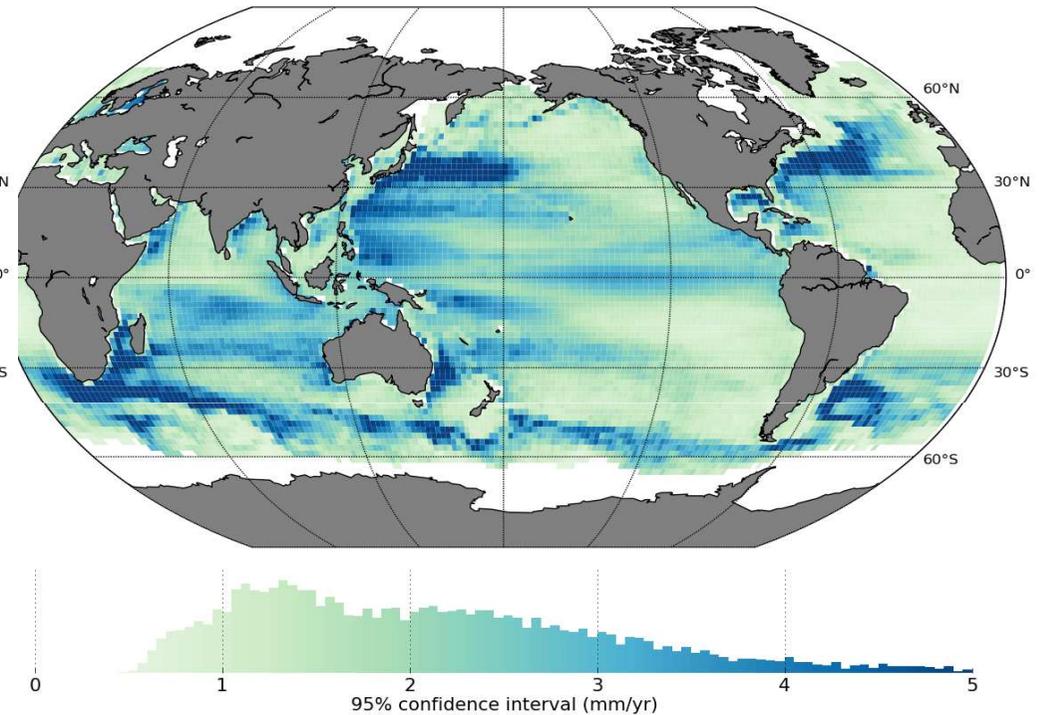


Comparing to OLS solution

OLS

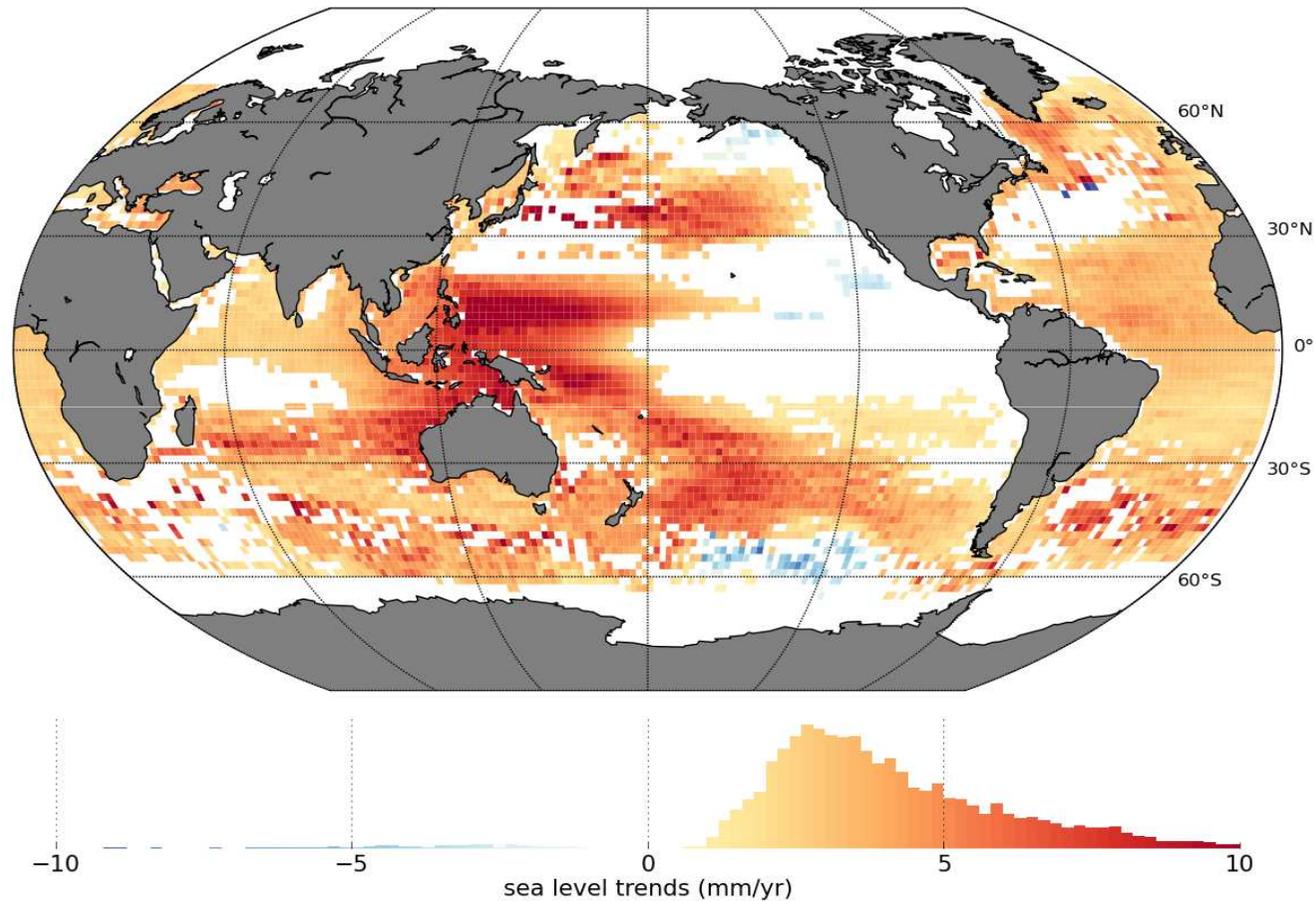


Full covariance



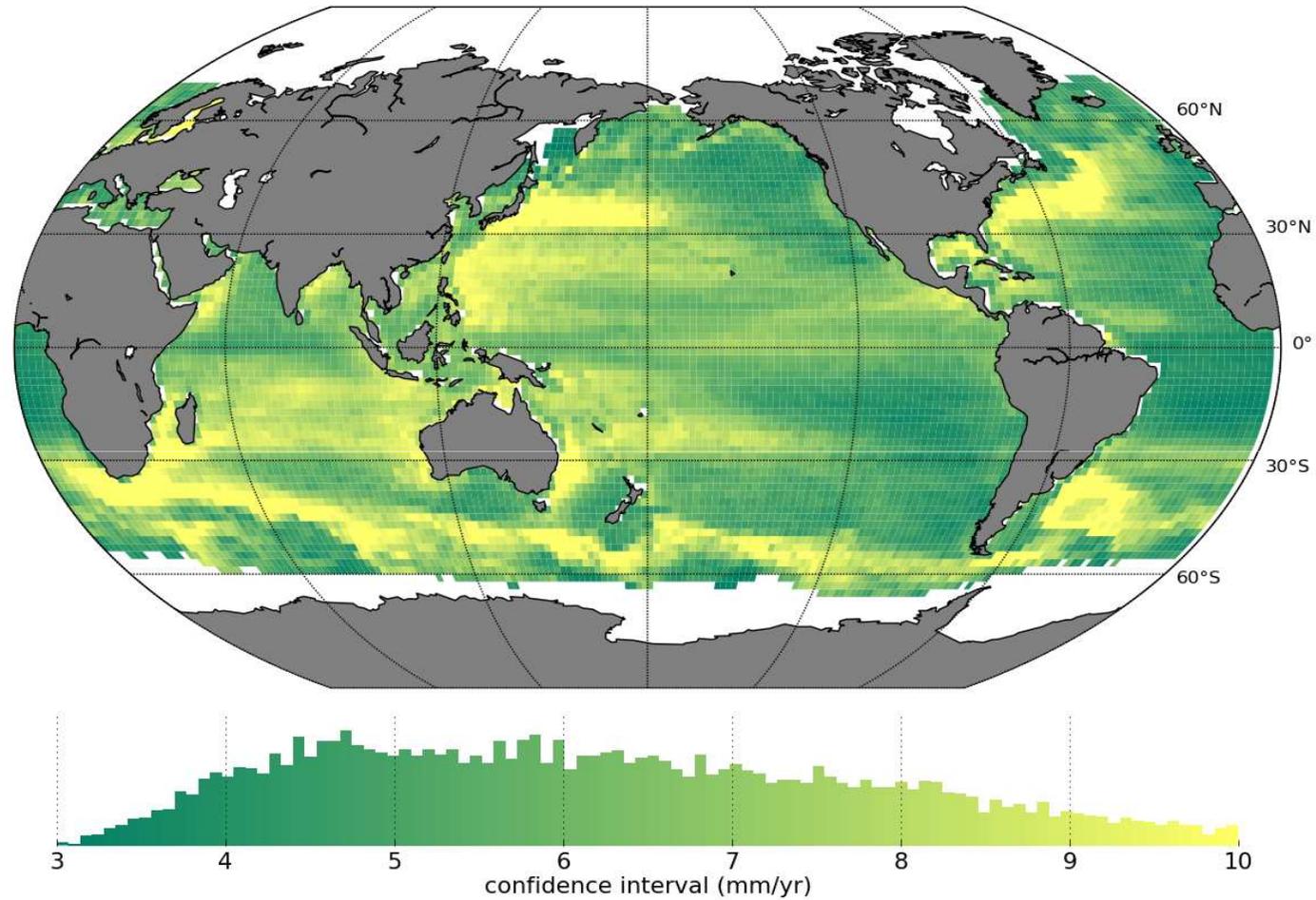
Significant trends

Places where we can reject the hypothesis that there is no trend



67 % of the ocean

Including ocean variability



Conclusions

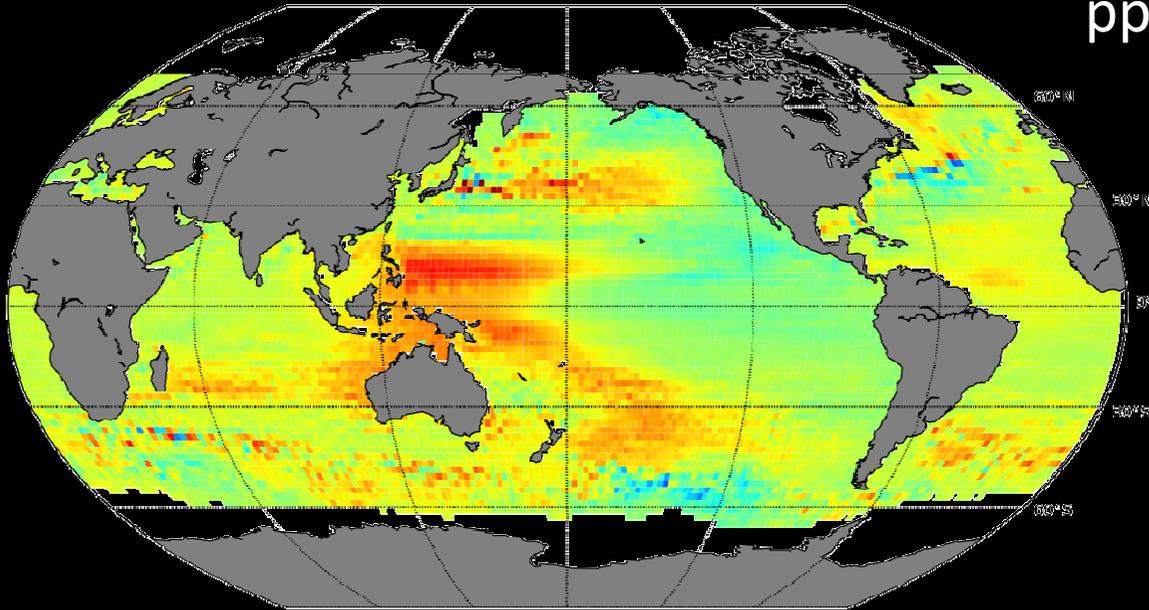
- Method provides a map of trend uncertainties,
 - Systematic uncertainties range between **1 to 3 mm/yr**
 - More realistic confidence interval than OLS,
-
- Results depend on the *a priori* description of errors,
 - If the error model is wrong, the results are
 - Accurate error covariance description is crucial
 - With time, the CI will reduce

Outlook

- Introduce noise heteroskedasticity,
i.e. larger errors on TOPEX than Jason-2 ?
- Introduce natural ocean variability
i.e. given the natural low frequency variability of SL, can we detect climatic trends ?
or are the patterns observed likely to be stable in time (*e.g.* Meyssignac et al. 2012) ?

Questions ?

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